



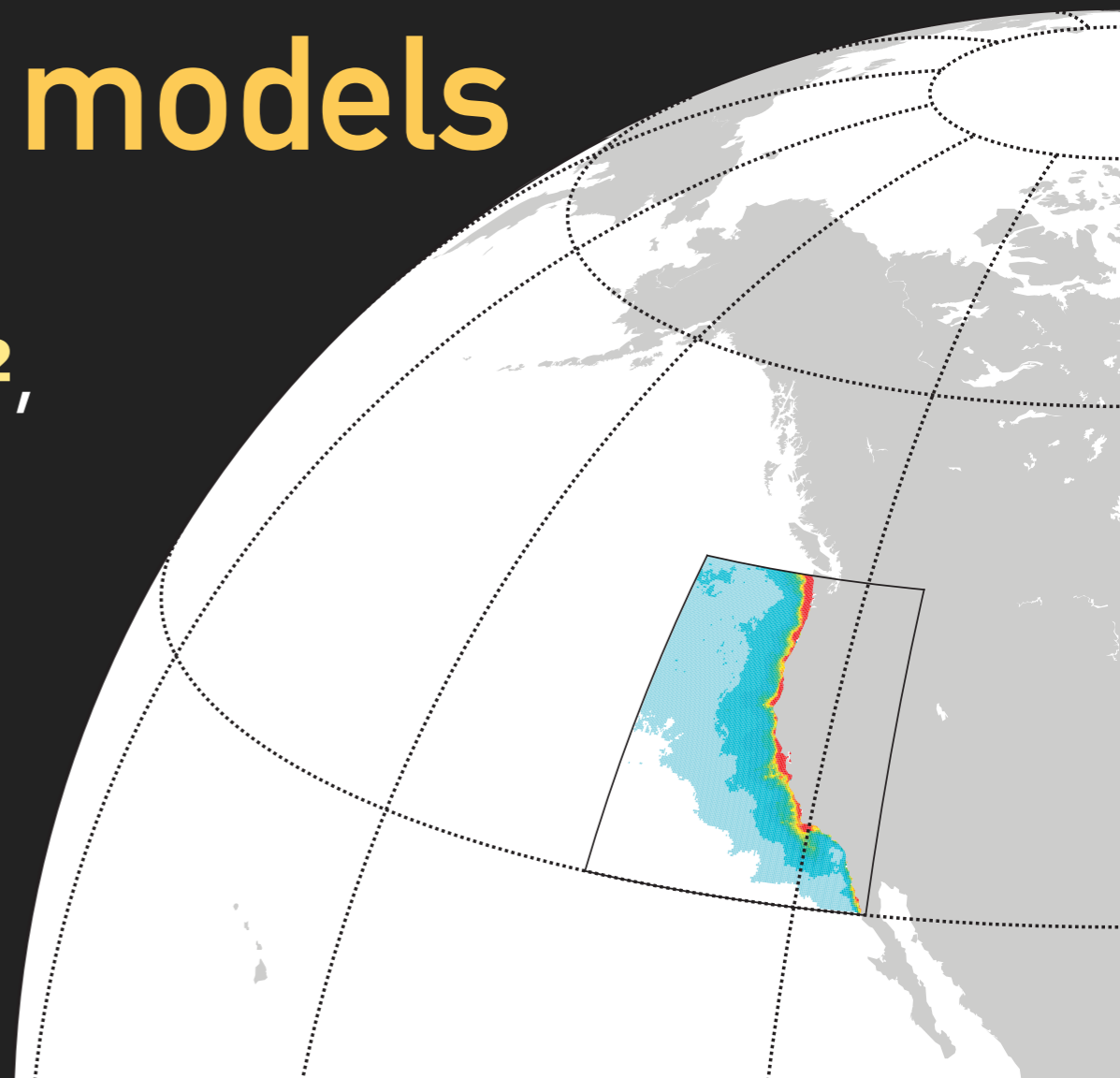
PICES-2018 Annual Meeting

# Data assimilation of physical and chlorophyll observations in the California Current System using two biogeochemical models

Jann Paul Mattern<sup>1</sup>, **Hajoon Song<sup>2</sup>**,  
Chris A. Edwards<sup>1</sup>, Andy Moore<sup>1</sup>  
and Jerome Fiechter<sup>1</sup>

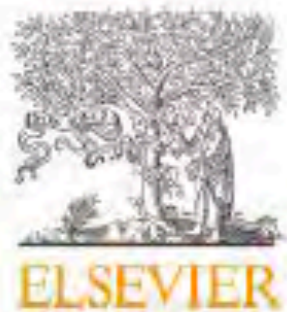
1. Department of Ocean Sciences, UCSC

2. Department of Atmospheric Sciences,  
Yonsei University, Korea



# Data assimilation of physical and chlorophyll observations in the California Current System using two biogeochemical models

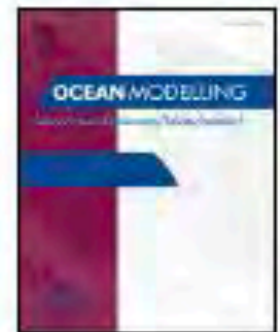
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Data assimilation of physical and chlorophyll *a* observations in the California Current System using two biogeochemical models



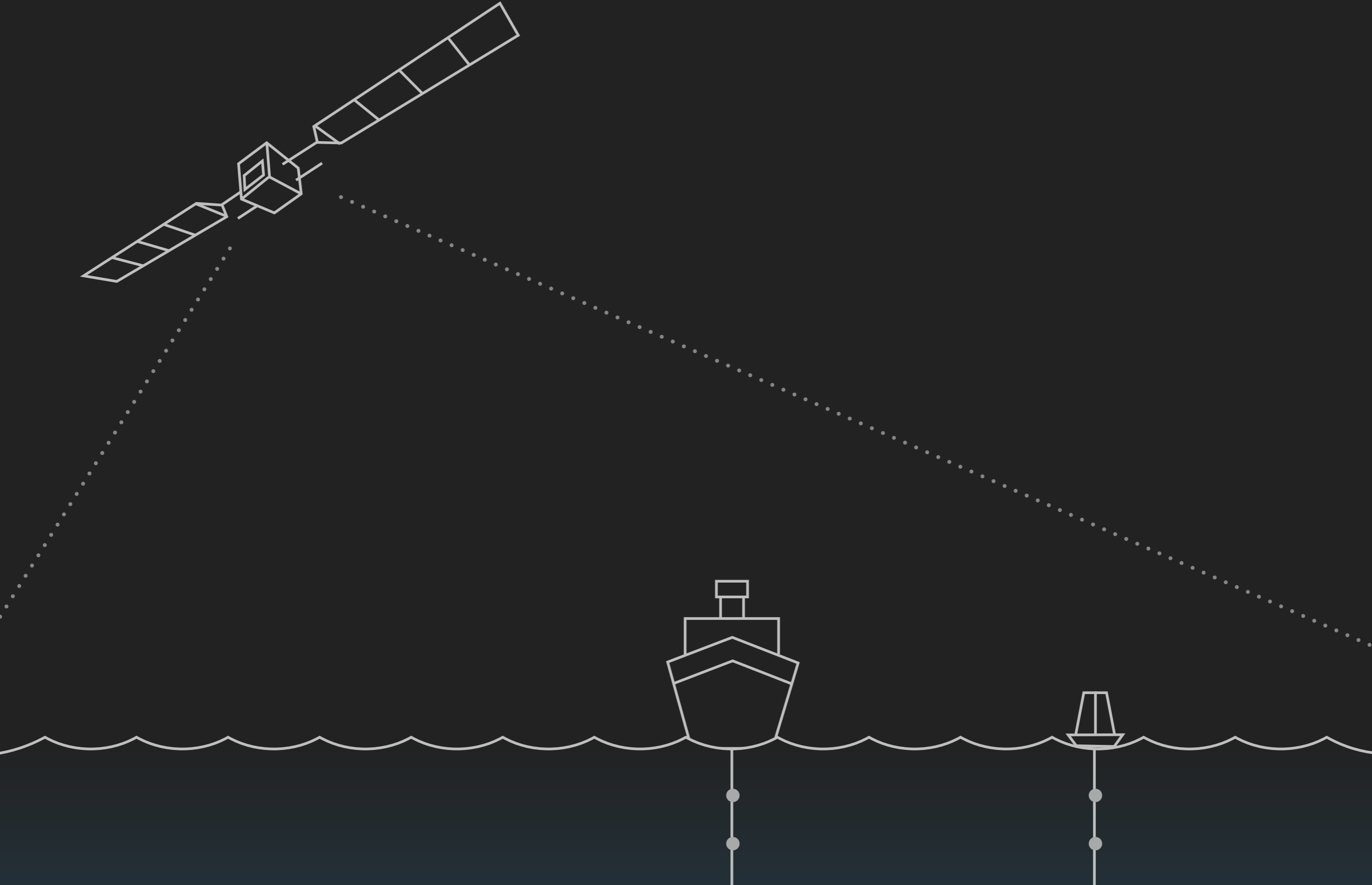
Jann Paul Mattern<sup>a,\*</sup>, Hajoon Song<sup>b</sup>, Christopher A. Edwards<sup>a</sup>, Andrew M. Moore<sup>a</sup>, Jerome Fiechter<sup>a</sup>

<sup>a</sup> Department of Ocean Sciences, University of California, Santa Cruz, California, USA

<sup>b</sup> Department of Earth, Atmospheric and Planetary Sciences, Massachusetts Institute of Technology, Massachusetts, USA

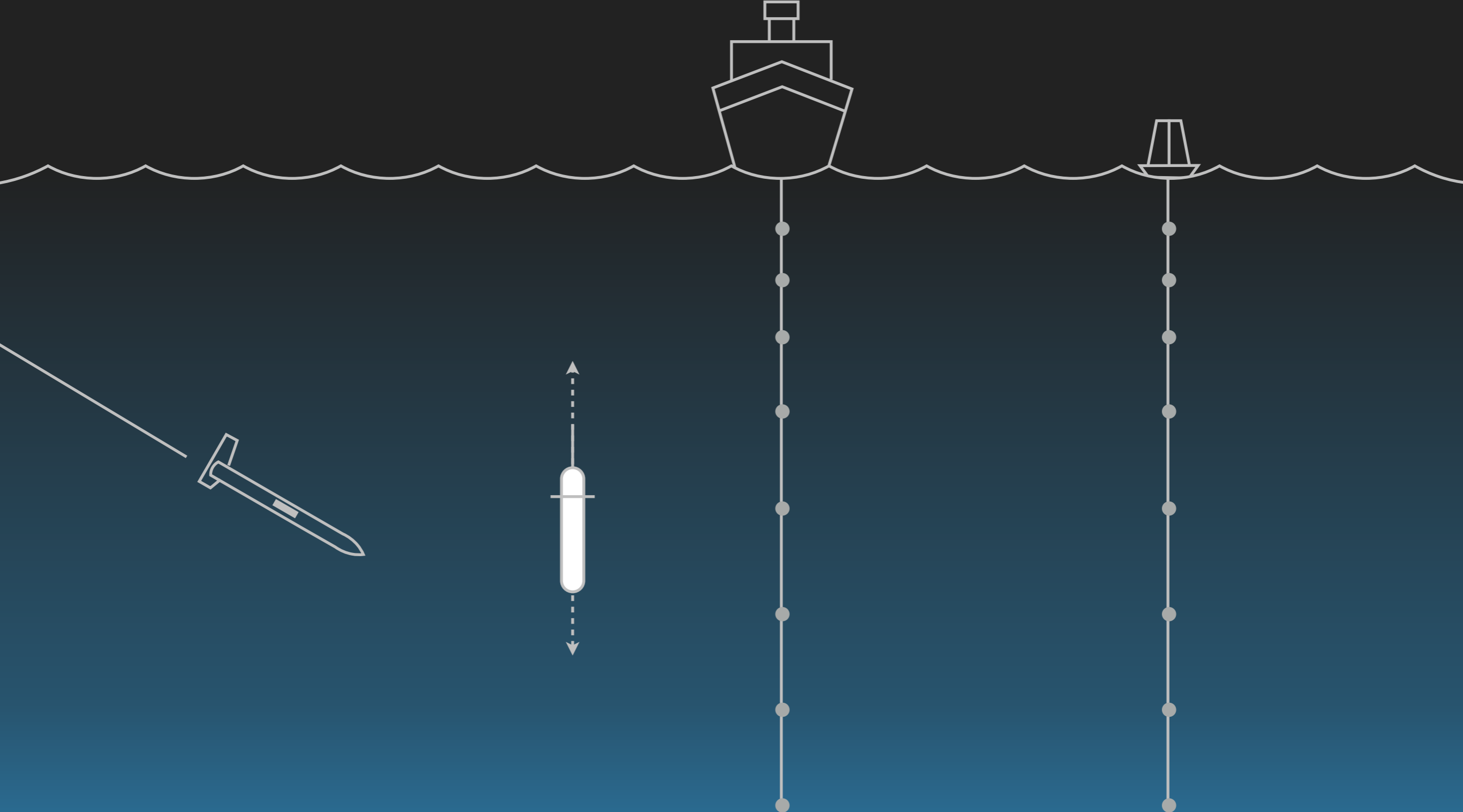
# DATA ASSIMILATION: OBSERVATIONS

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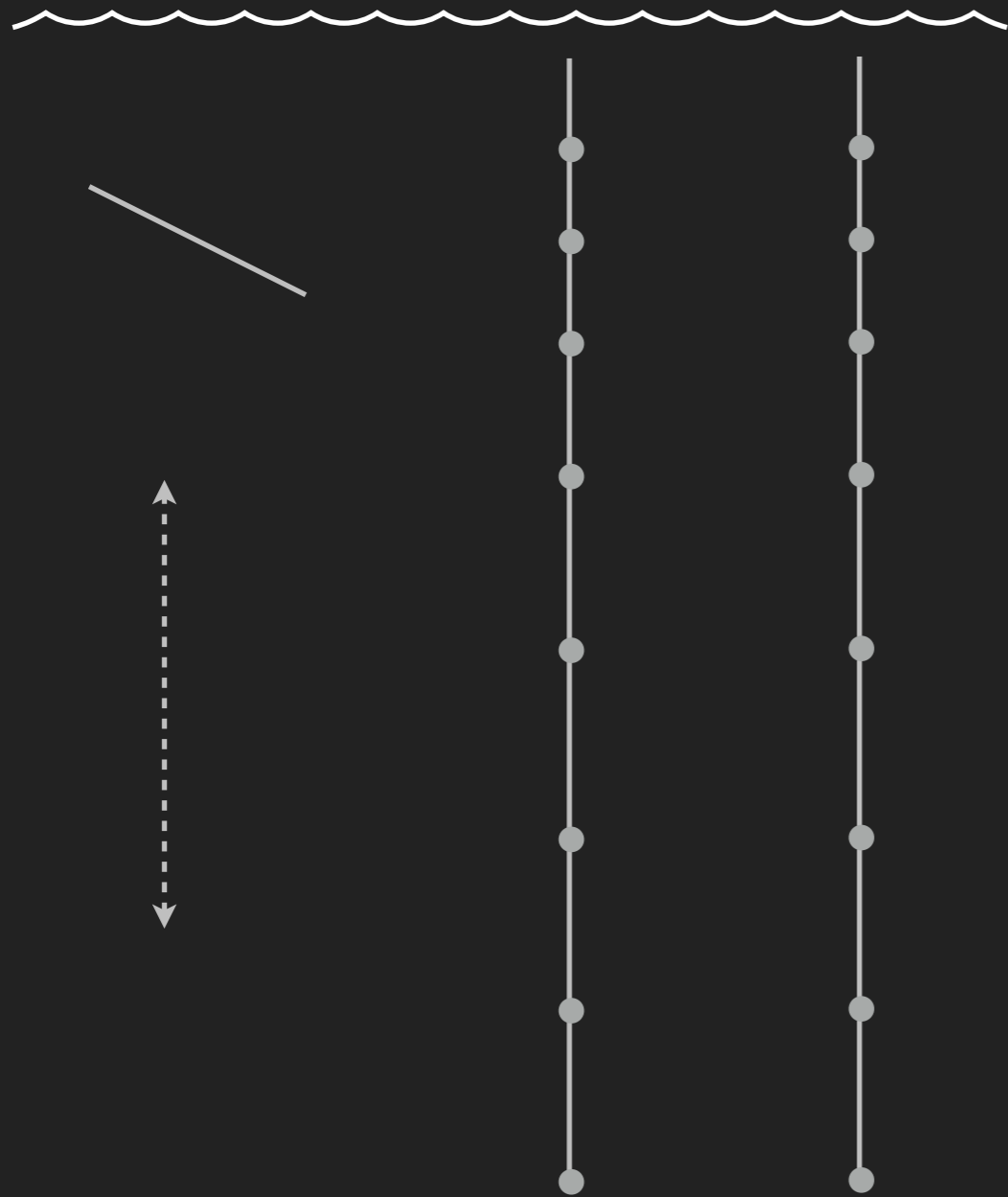
# DATA ASSIMILATION: OBSERVATIONS

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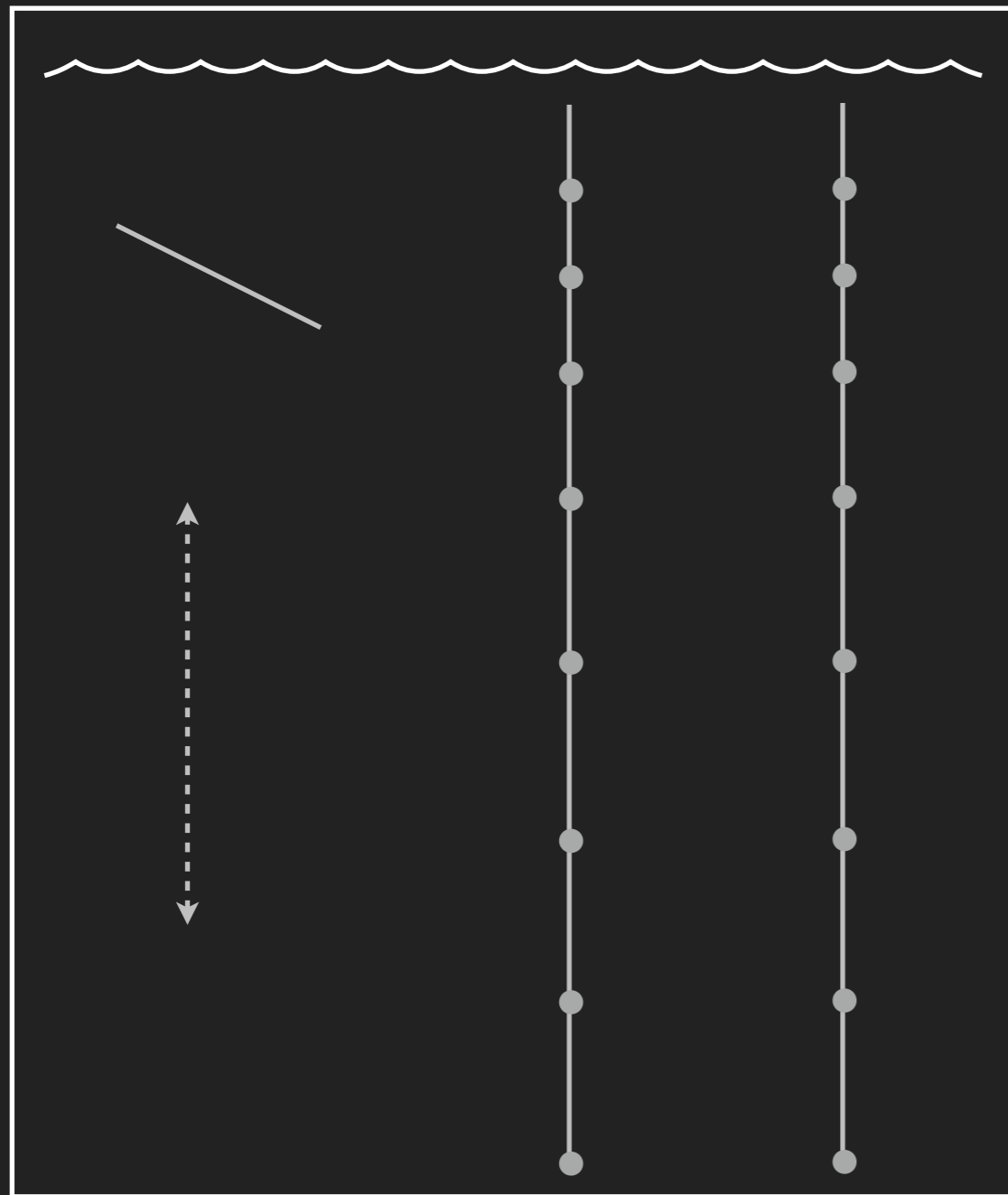
# DATA ASSIMILATION: COMBINING THE OBSERVATIONS AND THE MODEL

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# DATA ASSIMILATION: COMBINING THE OBSERVATIONS AND THE MODEL

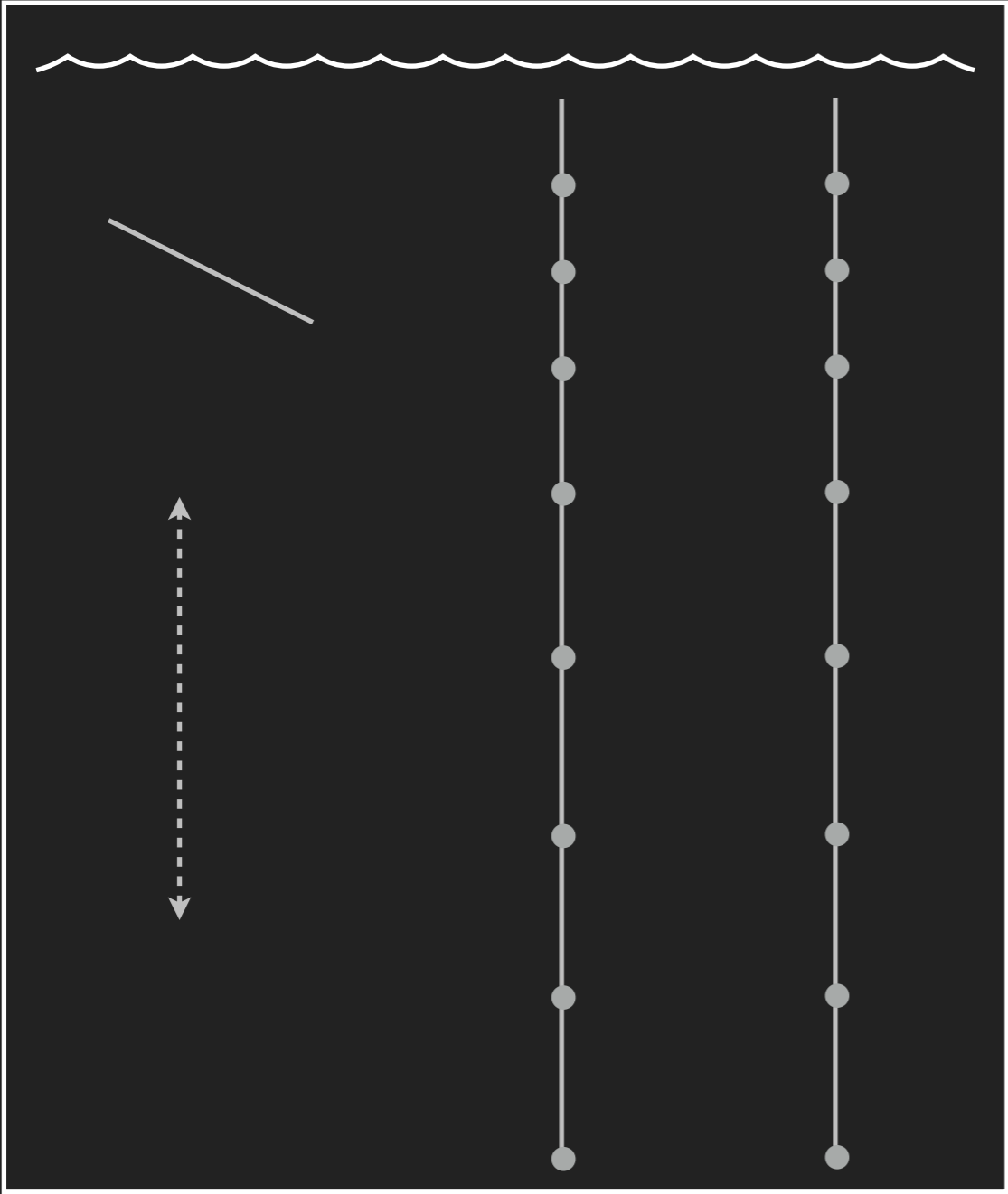
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Observations

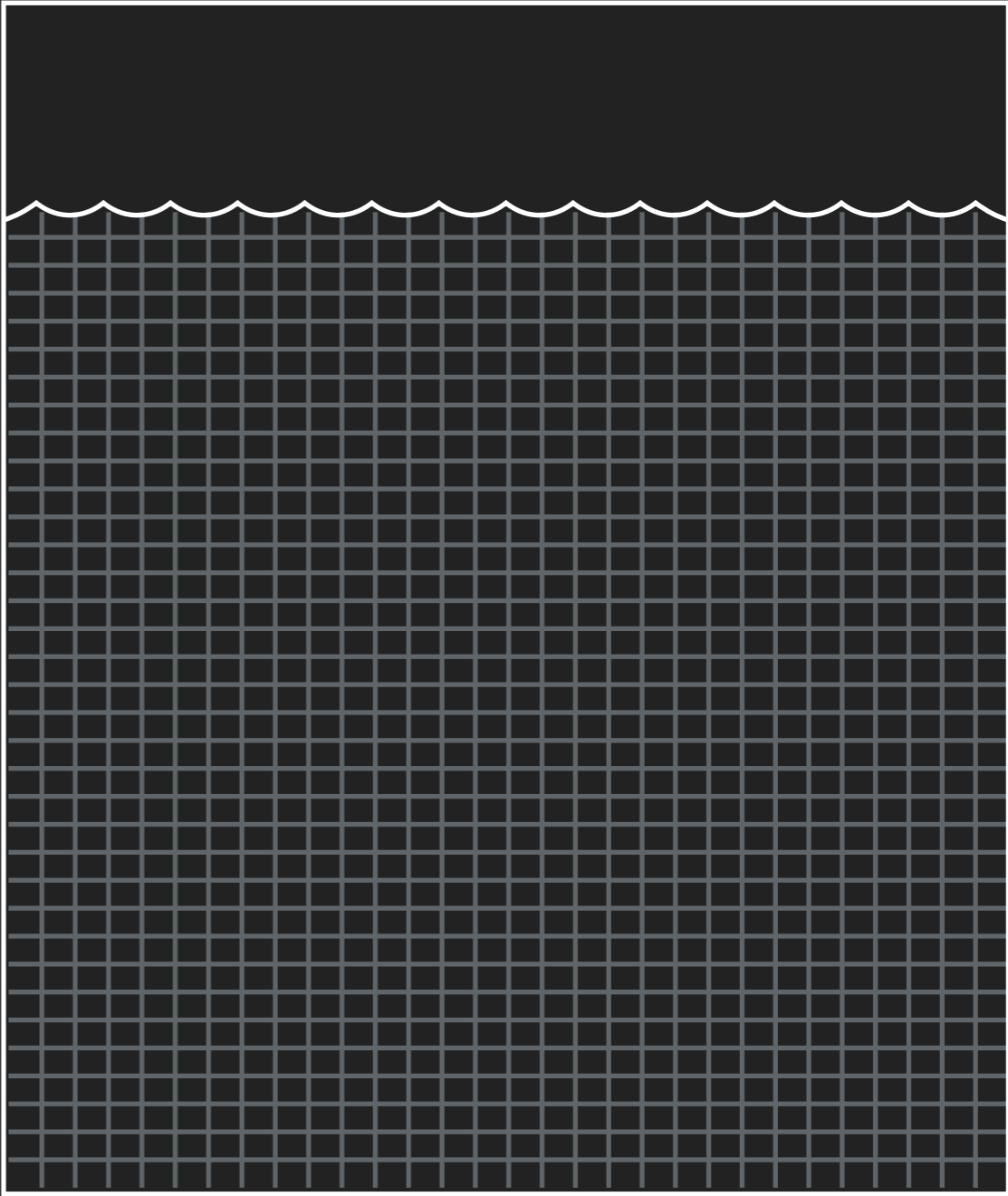
# DATA ASSIMILATION: COMBINING THE OBSERVATIONS AND THE MODEL

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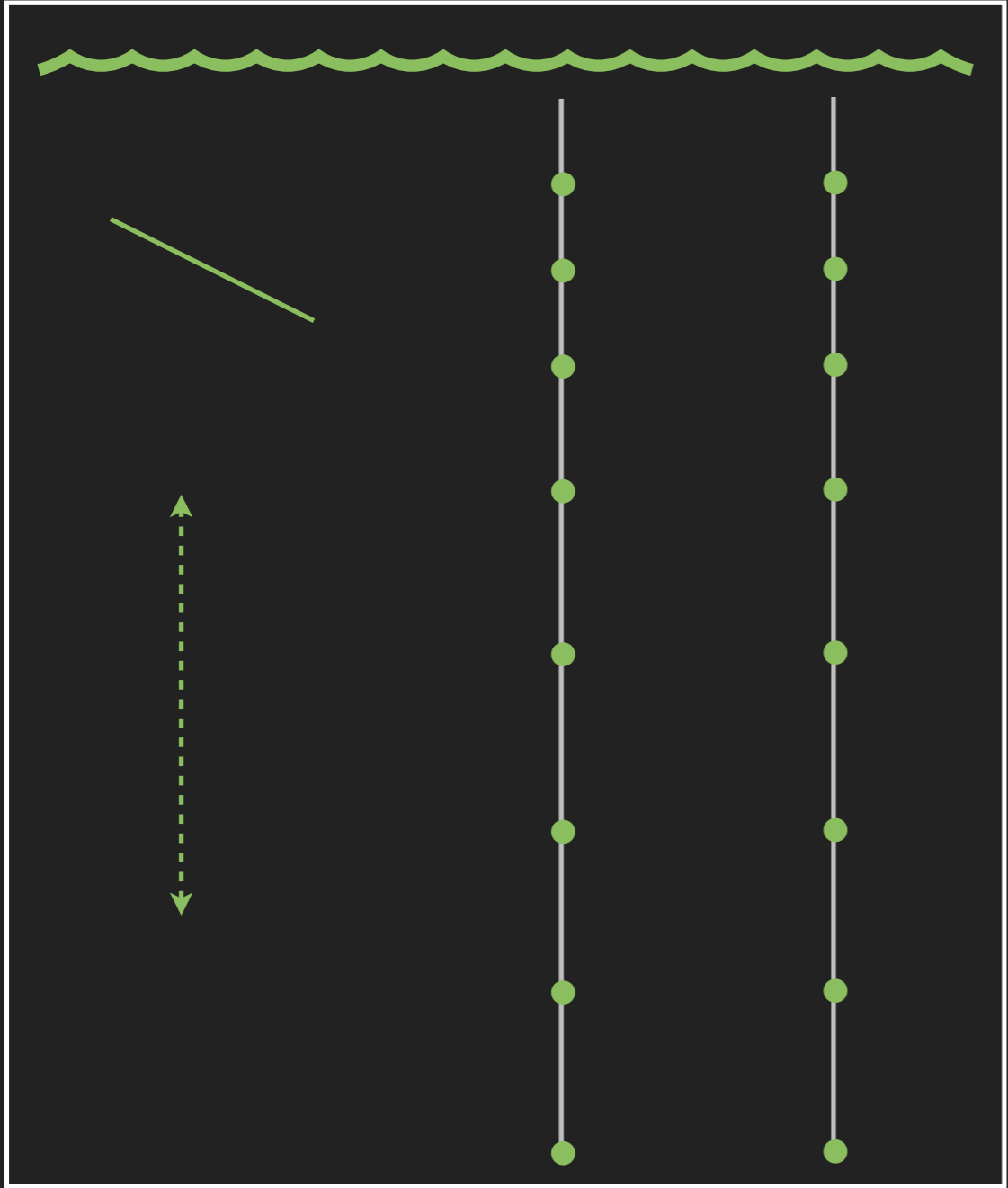
Observations

+



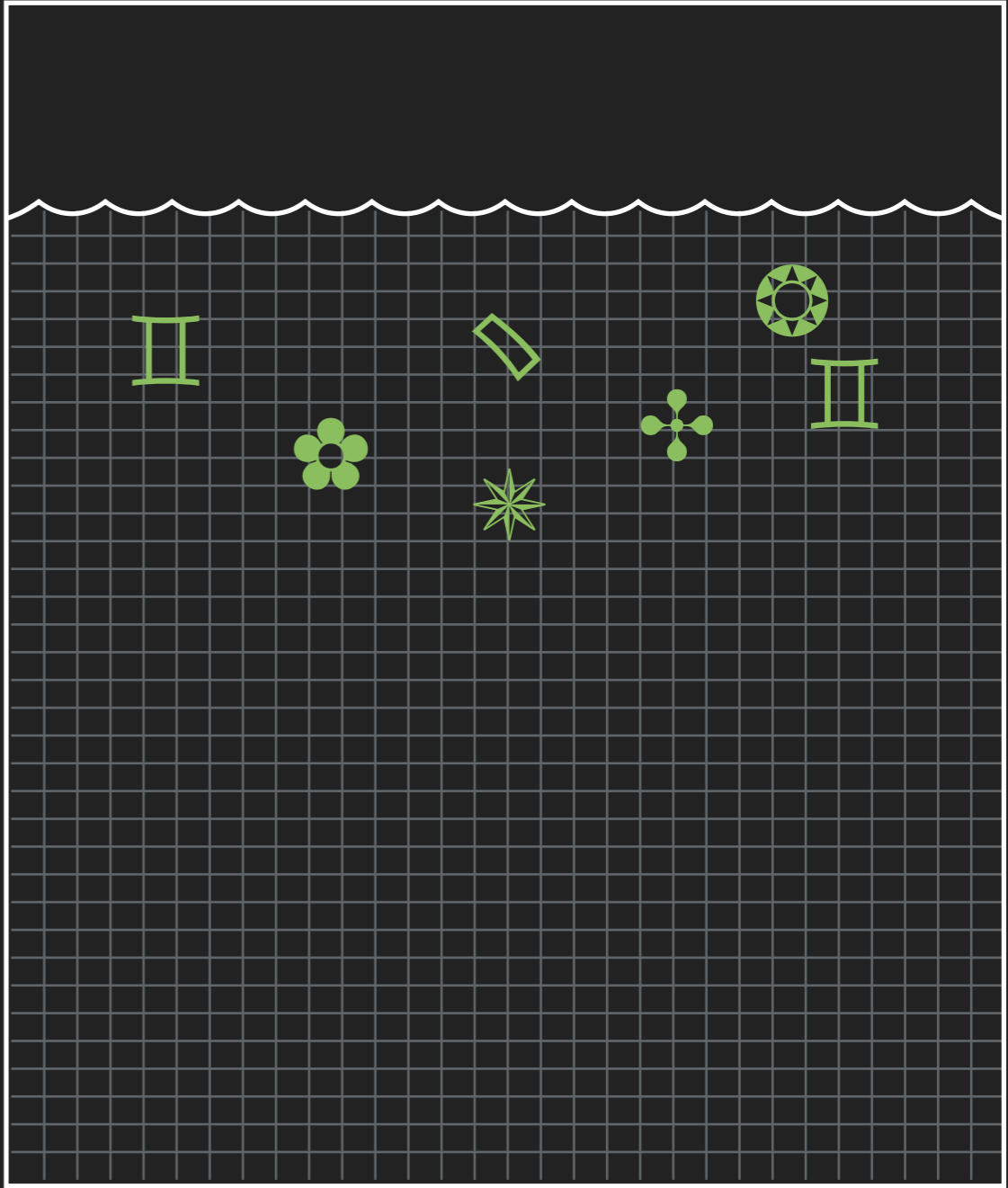
Numerical model

# DATA ASSIMILATION: PHYSICAL AND BIOGEOCHEMICAL COUPLED MODEL



Observations

+



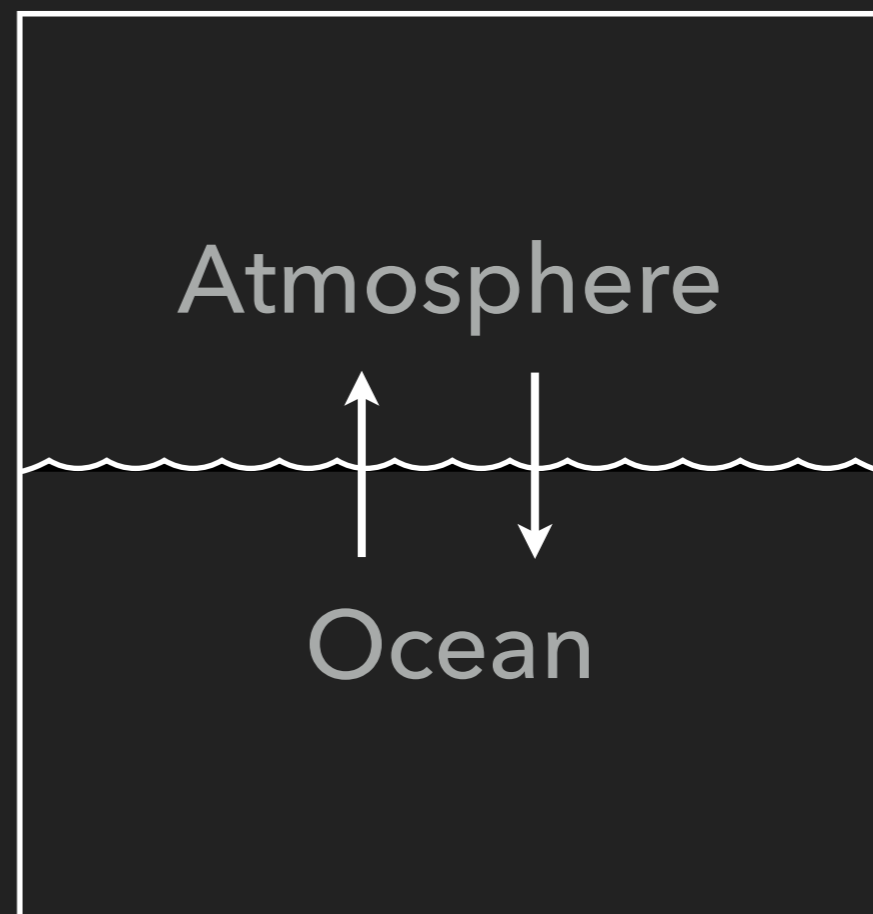
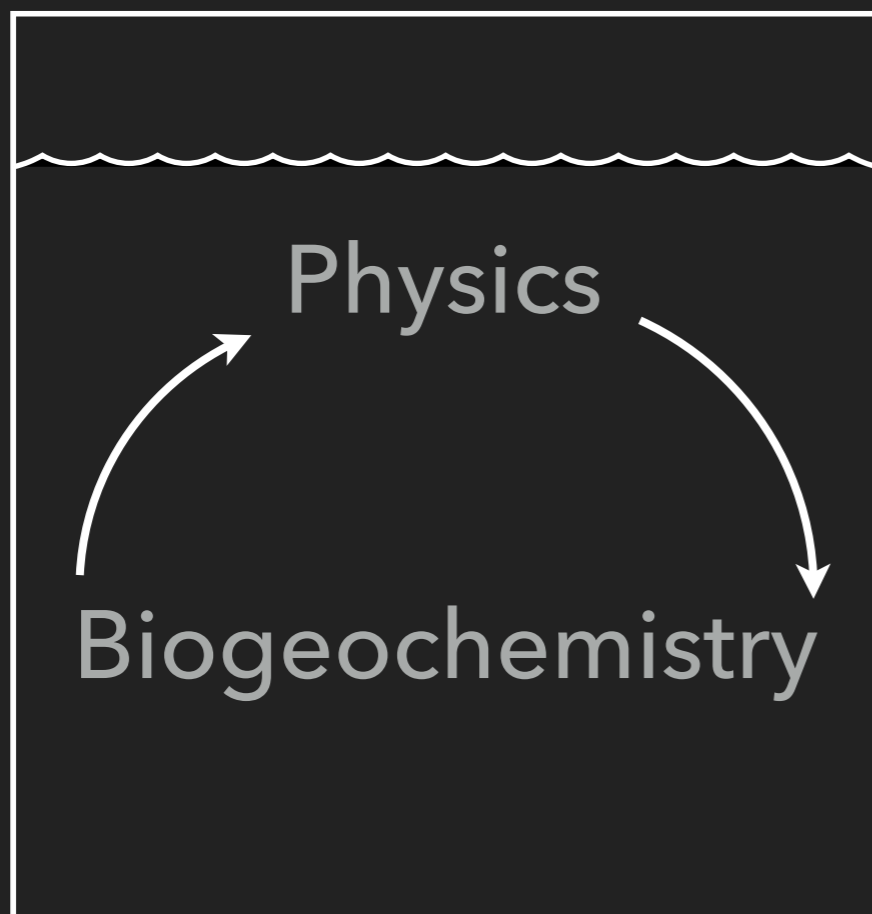
Numerical model



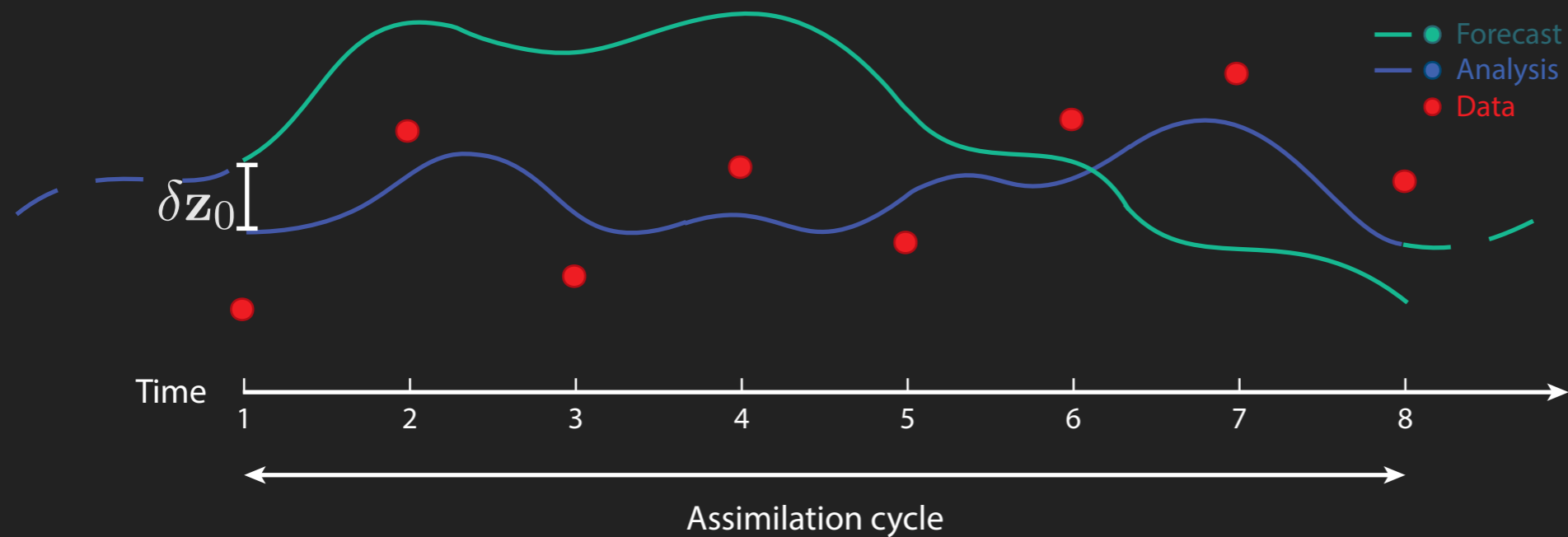
## WHY COUPLED PHYSICAL-BIOGEOCHEMICAL DATA ASSIMILATION?

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- ▶ Many applications : Fishery management ...
- ▶ Remove errors from the physical data assimilation
- ▶ A good testbed for the coupled data assimilation



# Data assimilation : incremental 4-D variational method



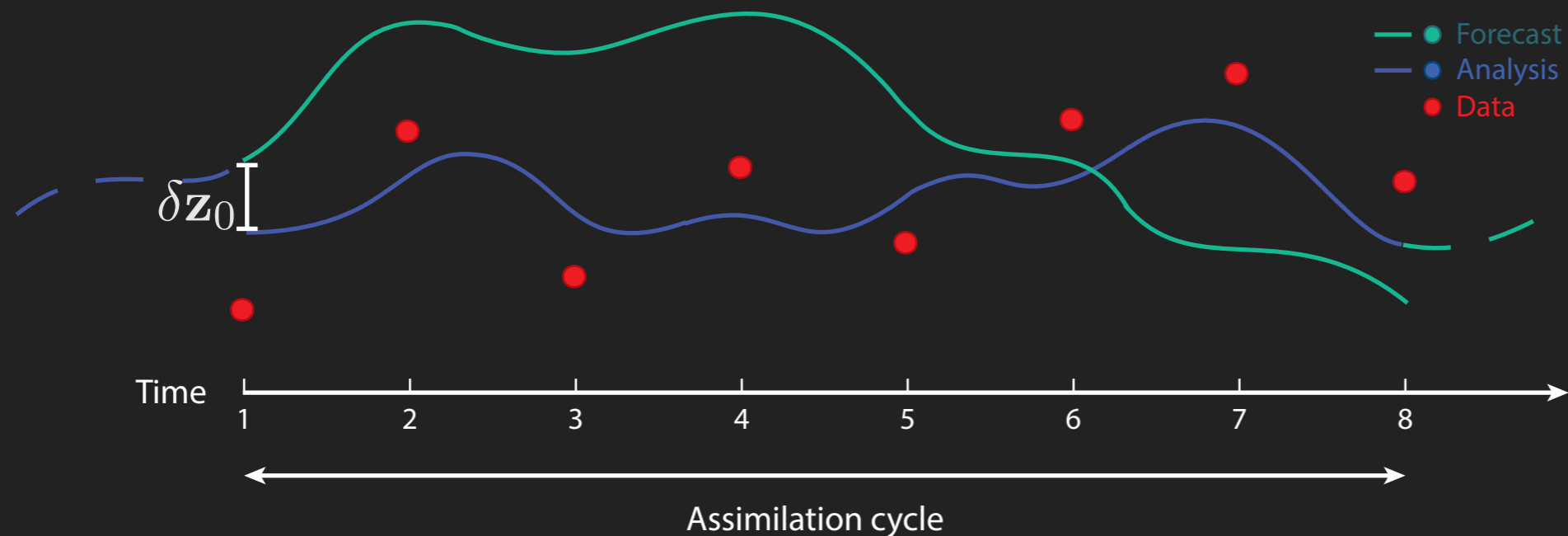
Edwards et al., 2015

$$J(\delta \mathbf{z}_0) = \frac{1}{2} \delta \mathbf{z}_0^T \mathbf{B}^{-1} \delta \mathbf{z}_0 + \frac{1}{2} \sum_{i=1}^{N_o} (\mathbf{d}_i - \mathbf{H}_i \mathbf{M}_{i,0} \delta \mathbf{z}_0)^T \mathbf{R}_i^{-1} (\mathbf{d}_i - \mathbf{H}_i \mathbf{M}_{i,0} \delta \mathbf{z}_0)$$

Courtier et al., 1994

$$\delta \mathbf{z}_0 = \mathbf{z}_{0,a} - \mathbf{z}_{0,b}$$

# Data assimilation : incremental 4-D variational method



Edwards et al., 2015

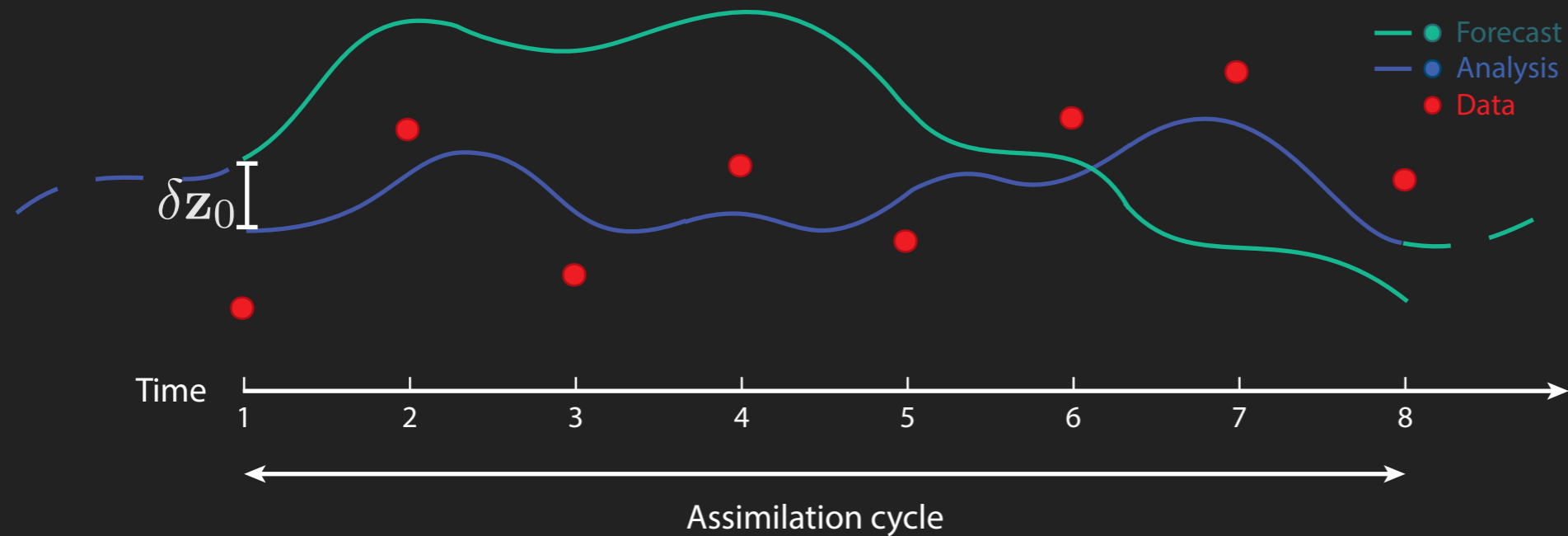
$$J(\delta \mathbf{z}_0) = \frac{1}{2} \delta \mathbf{z}_0^T \mathbf{B}^{-1} \delta \mathbf{z}_0 + \frac{1}{2} \sum_{i=1}^{N_o} (\mathbf{d}_i - \mathbf{H}_i \mathbf{M}_{i,0} \delta \mathbf{z}_0)^T \mathbf{R}_i^{-1} (\mathbf{d}_i - \mathbf{H}_i \mathbf{M}_{i,0} \delta \mathbf{z}_0)$$

Courtier et al., 1994

$$\delta \mathbf{z}_0 = \mathbf{B} \mathbf{M}^T \mathbf{H}^T (\mathbf{H} \mathbf{M} \mathbf{B} \mathbf{M}^T \mathbf{H}^T + \mathbf{R}^{-1})^{-1} \mathbf{d}$$

↑  
minimizes  $J$

# Data assimilation : incremental 4-D variational method



Edwards et al., 2015

$$J(\delta \mathbf{z}_0) = \frac{1}{2} \delta \mathbf{z}_0^T \mathbf{B}^{-1} \delta \mathbf{z}_0 + \frac{1}{2} \sum_{i=1}^{N_o} (\mathbf{d}_i - \mathbf{H}_i \mathbf{M}_{i,0} \delta \mathbf{z}_0)^T \mathbf{R}_i^{-1} (\mathbf{d}_i - \mathbf{H}_i \mathbf{M}_{i,0} \delta \mathbf{z}_0)$$

Courtier et al., 1994

$$\delta \mathbf{z}_0 = \mathbf{B} \mathbf{M}^T \mathbf{H}^T \left( \mathbf{H} \mathbf{M} \mathbf{B} \mathbf{M}^T \mathbf{H}^T + \mathbf{R}^{-1} \right)^{-1} \mathbf{d}$$

$$\delta \mathbf{z}_0 = \mathbf{B} \mathbf{M}^T \hat{\mathbf{d}}$$

## COUPLED DATA ASSIMILATION IN EQUATIONS

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$$\delta \mathbf{z}_0 = \hat{\mathbf{B}} \mathbf{M}^T \hat{\mathbf{d}}$$

## COUPLED DATA ASSIMILATION IN EQUATIONS

---

$$\delta \mathbf{z}_0 = \hat{\mathbf{B}} \mathbf{M}^T \hat{\mathbf{d}}$$

$\downarrow$

$$\mathbf{M} = \begin{bmatrix} \mathbf{M}_{phy} & \mathbf{M}_{b,p} \\ \mathbf{M}_{p,b} & \mathbf{M}_{bio} \end{bmatrix}$$

$$\delta \mathbf{z}_0 = \hat{\mathbf{B}} \mathbf{M}^T \hat{\mathbf{d}}$$

$$\mathbf{M} = \begin{bmatrix} \mathbf{M}_{phy} & \mathbf{M}_{b,p} \\ \mathbf{M}_{p,b} & \mathbf{M}_{bio} \end{bmatrix}$$

## Coupled data assimilation

$$\begin{bmatrix} \delta \mathbf{x}_{phy} \\ \delta \mathbf{x}_{bio} \end{bmatrix} = \begin{bmatrix} \hat{\mathbf{B}}_{phy} & 0 \\ 0 & \hat{\mathbf{B}}_{bio} \end{bmatrix} \begin{bmatrix} \mathbf{M}_{phy}^T & \mathbf{M}_{p,b}^T \\ \mathbf{M}_{b,p}^T & \mathbf{M}_{bio}^T \end{bmatrix} \begin{bmatrix} \hat{\mathbf{d}}_{phy} \\ \hat{\mathbf{d}}_{bio} \end{bmatrix}$$

## COUPLED DATA ASSIMILATION IN EQUATIONS

---

$$\delta \mathbf{z}_0 = \hat{\mathbf{B}} \mathbf{M}^T \hat{\mathbf{d}} \quad \text{No feedback from BGC to physics}$$

$\downarrow$

$$\mathbf{M} = \begin{bmatrix} \mathbf{M}_{phy} & \mathbf{0} \\ \mathbf{M}_{p,b} & \mathbf{M}_{bio} \end{bmatrix}$$

$\uparrow$

### Coupled data assimilation

$$\begin{bmatrix} \delta \mathbf{x}_{phy} \\ \delta \ln \mathbf{x}_{bio} \end{bmatrix}_0 = \begin{bmatrix} \hat{\mathbf{B}}_{phy} & \mathbf{0} \\ \mathbf{0} & \hat{\mathbf{B}}_{\ln bio} \end{bmatrix} \begin{bmatrix} \mathbf{M}_{phy}^T & \mathbf{M}_{p,b}^T \\ \mathbf{0} & \mathbf{M}_{bio}^T \end{bmatrix} \begin{bmatrix} \hat{\mathbf{d}}_{phy} \\ \hat{\mathbf{d}}_{bio} \end{bmatrix}$$



$$\delta \mathbf{z}_0 = \hat{\mathbf{B}} \mathbf{M}^T \hat{\mathbf{d}} \quad \text{No feedback from BGC to physics}$$

$$\mathbf{M} = \begin{bmatrix} \mathbf{M}_{phy} & \mathbf{0} \\ \mathbf{M}_{p,b} & \mathbf{M}_{bio} \end{bmatrix}$$

## Coupled data assimilation

$$\begin{bmatrix} \delta \mathbf{x}_{phy} \\ \delta \ln \mathbf{x}_{bio} \end{bmatrix}_0 = \begin{bmatrix} \hat{\mathbf{B}}_{phy} & \mathbf{0} \\ \mathbf{0} & \hat{\mathbf{B}}_{\ln bio} \end{bmatrix} \begin{bmatrix} \mathbf{M}_{phy}^T & \mathbf{M}_{p,b}^T \\ \mathbf{0} & \mathbf{M}_{bio}^T \end{bmatrix} \begin{bmatrix} \hat{\mathbf{d}}_{phy} \\ \hat{\mathbf{d}}_{bio} \end{bmatrix}$$

$$= \begin{bmatrix} \hat{\mathbf{B}}_{phy} \mathbf{M}_{phy}^T \hat{\mathbf{d}}_{phy} + \hat{\mathbf{B}}_{phy} \mathbf{M}_{p,b}^T \hat{\mathbf{d}}_{bio} \\ \hat{\mathbf{B}}_{\ln bio} \mathbf{M}_{bio}^T \hat{\mathbf{d}}_{bio} \end{bmatrix}$$

## COUPLED DATA ASSIMILATION IN EQUATIONS

$$\delta \mathbf{z}_0 = \hat{\mathbf{B}} \mathbf{M}^T \hat{\mathbf{d}} \quad \text{No feedback from BGC to physics}$$

$\uparrow$

$$\mathbf{M} = \begin{bmatrix} \mathbf{M}_{phy} & \mathbf{0} \\ \mathbf{M}_{p,b} & \mathbf{M}_{bio} \end{bmatrix}$$

## Coupled data assimilation

$$\begin{bmatrix} \delta \mathbf{x}_{phy} \\ \delta \ln \mathbf{x}_{bio} \end{bmatrix}_0 = \begin{bmatrix} \hat{\mathbf{B}}_{phy} & \mathbf{0} \\ \mathbf{0} & \hat{\mathbf{B}}_{\ln bio} \end{bmatrix} \begin{bmatrix} \mathbf{M}_{phy}^T & \mathbf{M}_{p,b}^T \\ \mathbf{0} & \mathbf{M}_{bio}^T \end{bmatrix} \begin{bmatrix} \hat{\mathbf{d}}_{phy} \\ \hat{\mathbf{d}}_{bio} \end{bmatrix}$$

$$= \begin{bmatrix} \hat{\mathbf{B}}_{phy} \mathbf{M}_{phy}^T \hat{\mathbf{d}}_{phy} + \hat{\mathbf{B}}_{phy} \mathbf{M}_{p,b}^T \hat{\mathbf{d}}_{bio} \\ \hat{\mathbf{B}}_{\ln bio} \mathbf{M}_{bio}^T \hat{\mathbf{d}}_{bio} \end{bmatrix}$$

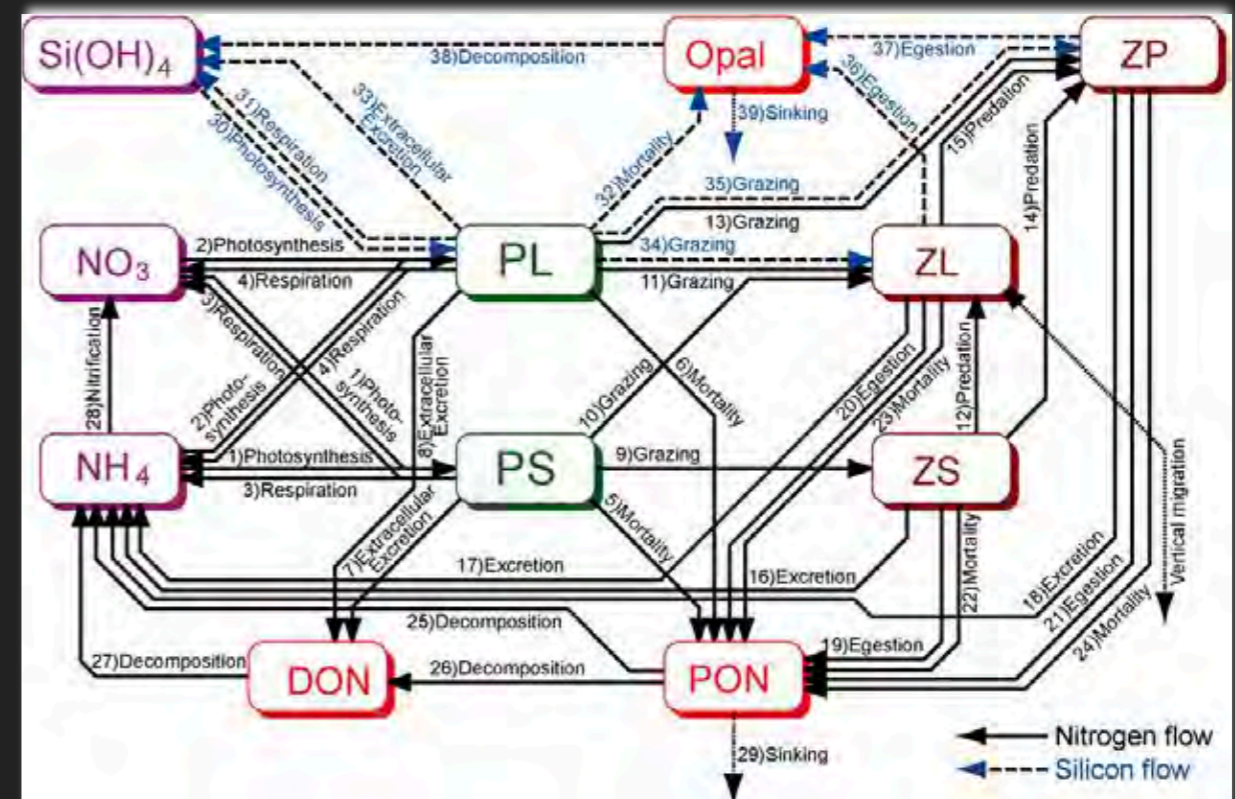
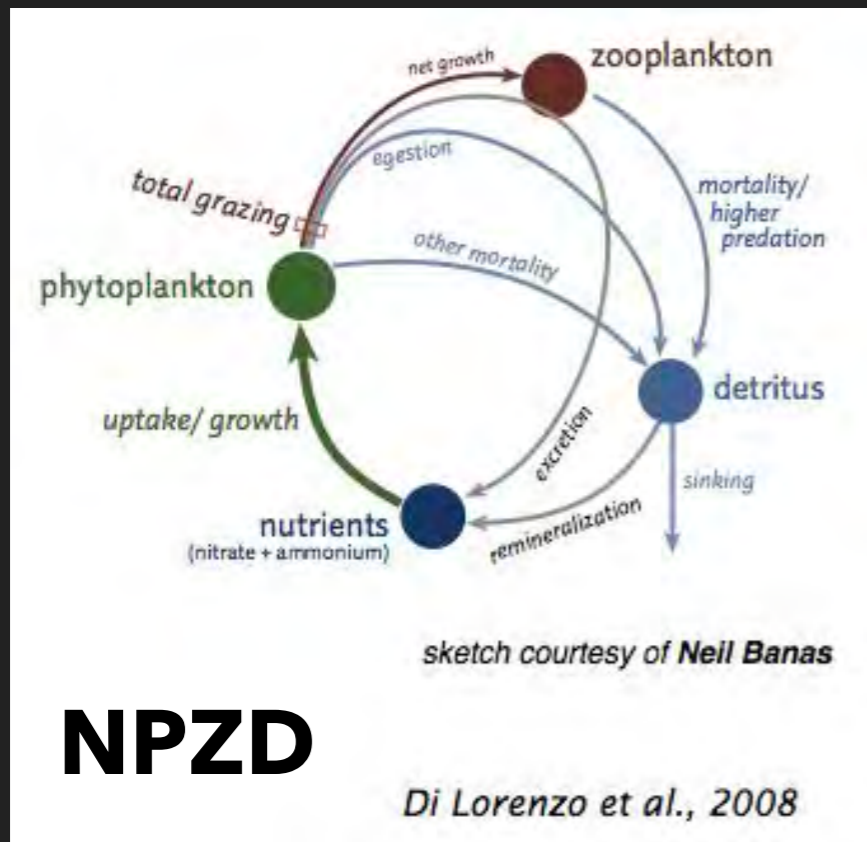
Chlorophyll observations can help improving ocean current estimation!!!

# COUPLED DATA ASSIMILATION IN EQUATIONS

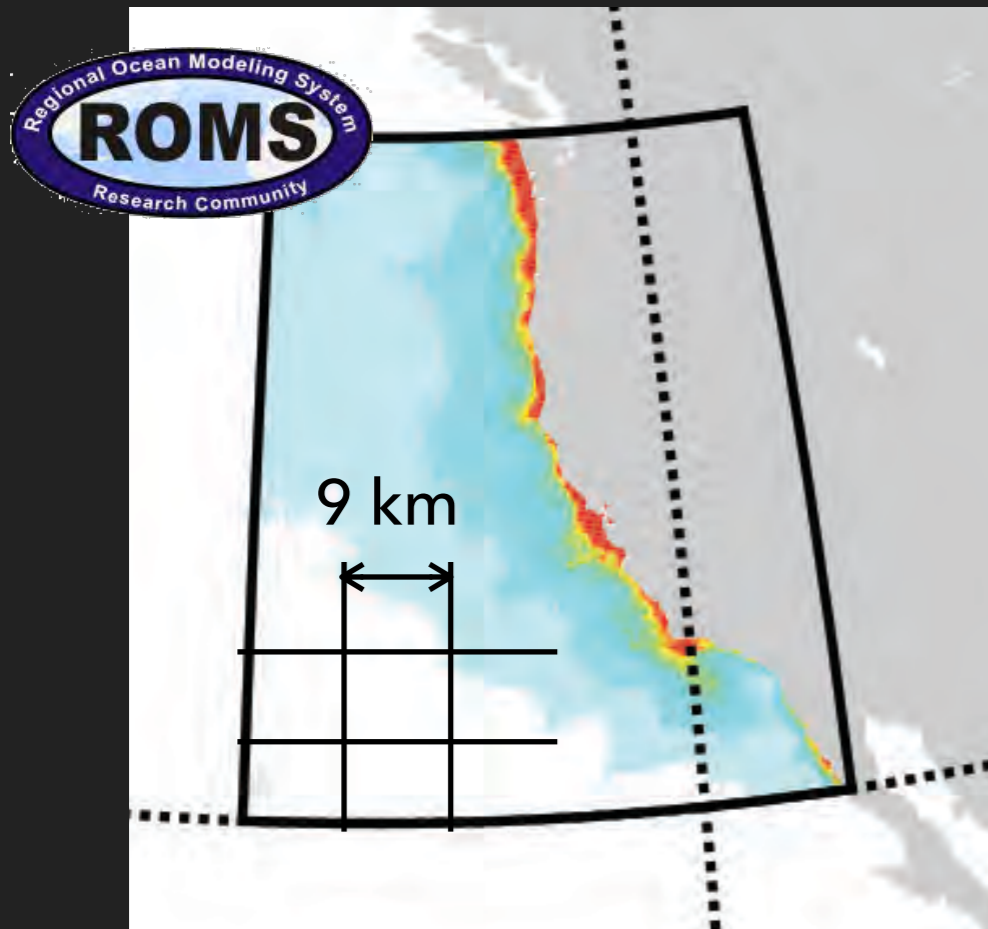
$$\delta \mathbf{z}_0 = \hat{\mathbf{B}} \mathbf{M}^T \hat{\mathbf{d}}$$

$$\mathbf{M} = \begin{bmatrix} \mathbf{M}_{phy} & \mathbf{0} \\ \mathbf{M}_{p,b} & \mathbf{M}_{bio} \end{bmatrix}$$

## NEMURO

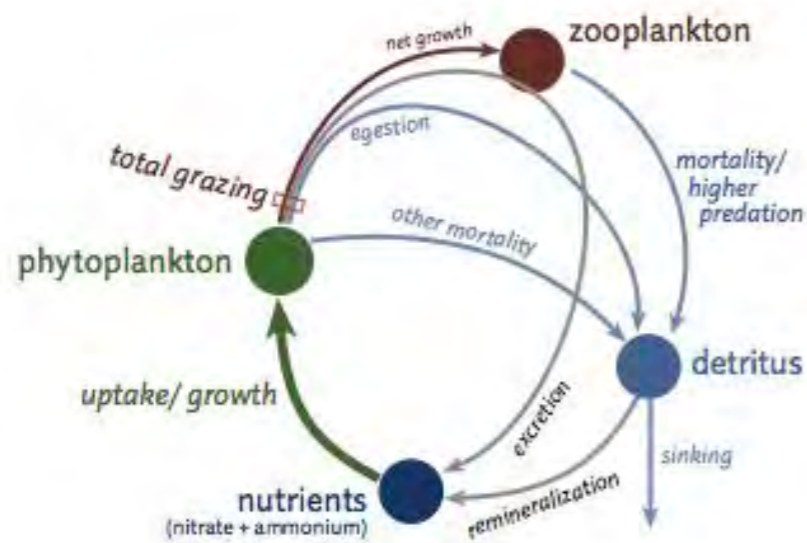


# COUPLED DATA ASSIMILATION OVER THE CCS



- ▶ 1 year experiment.
- ▶ Updating model states @ every 4 days
- ▶ SSH, SST, in situ T/S and surface chlorophyll

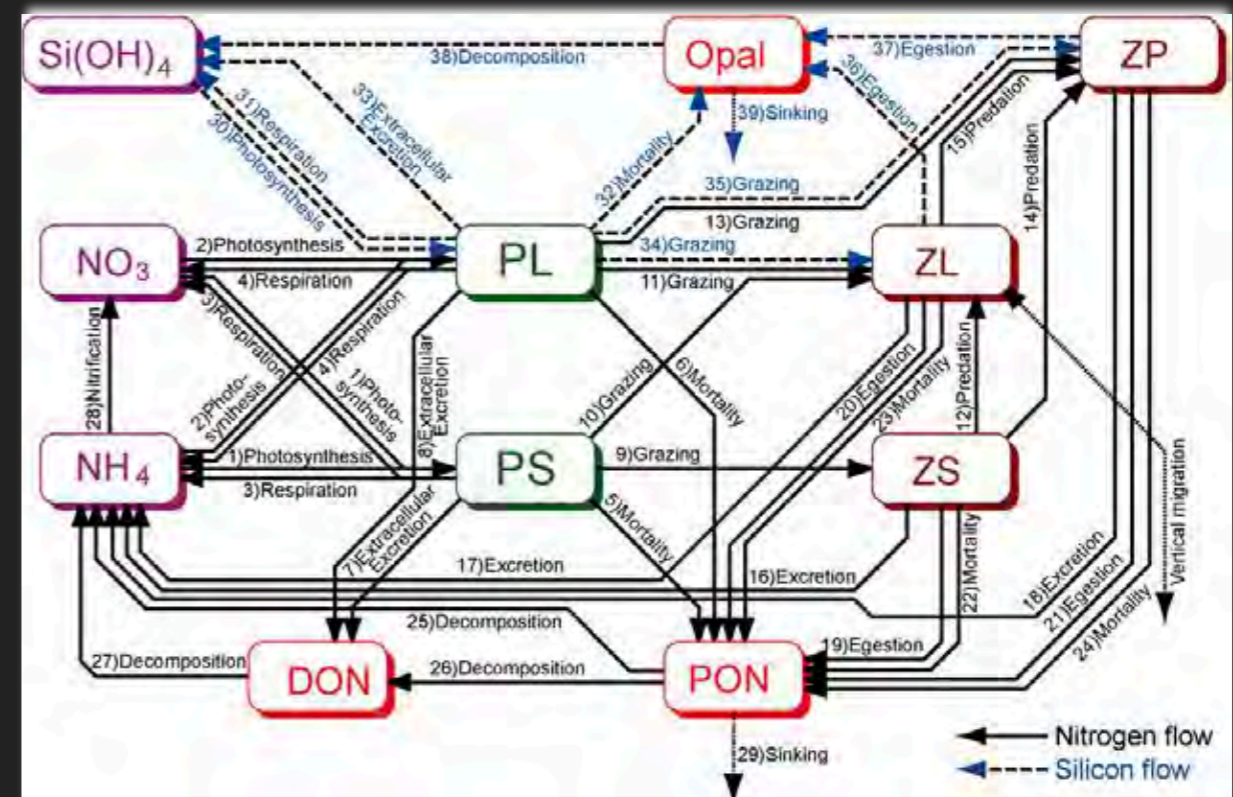
## NEMURO



sketch courtesy of Neil Banas

**NPZD**

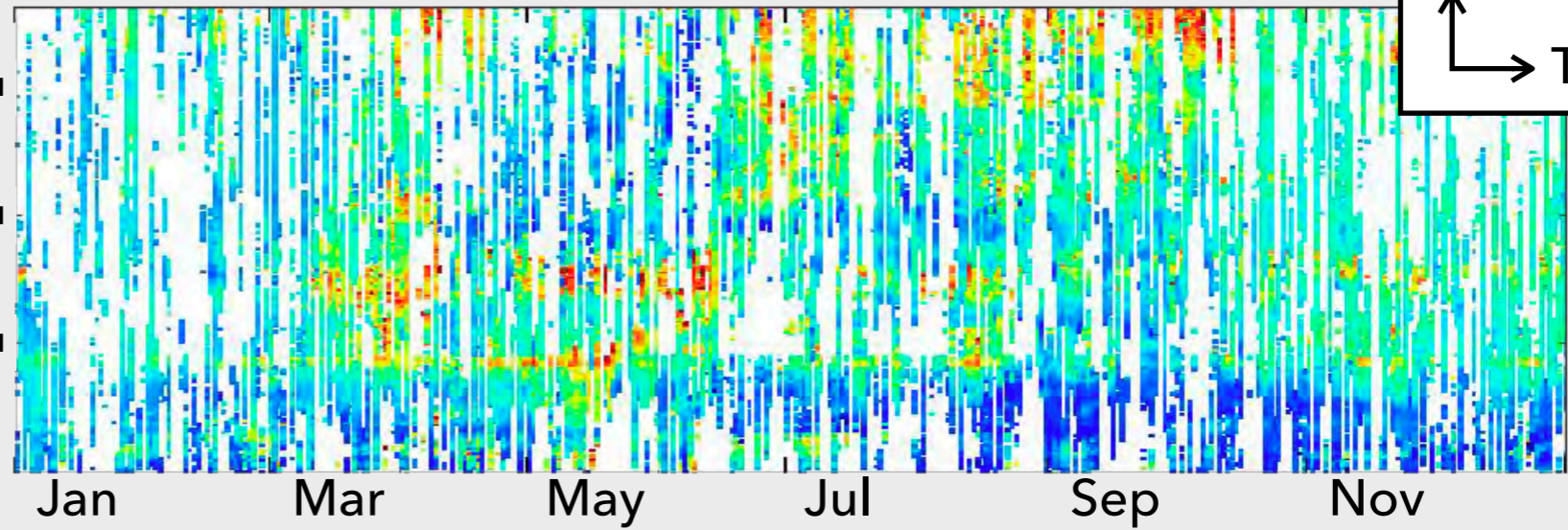
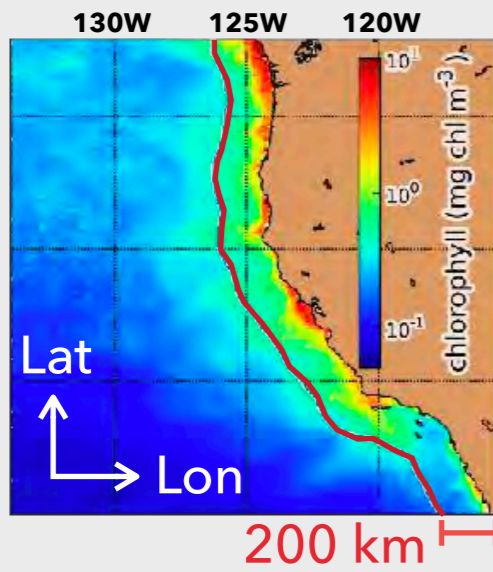
Di Lorenzo et al., 2008



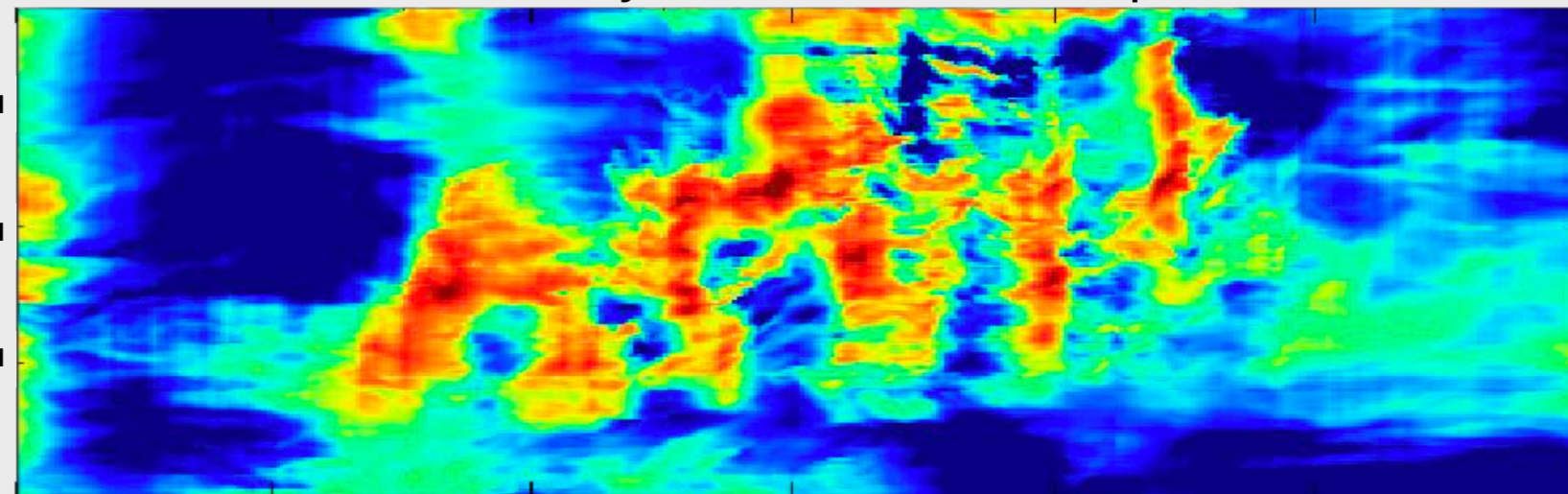
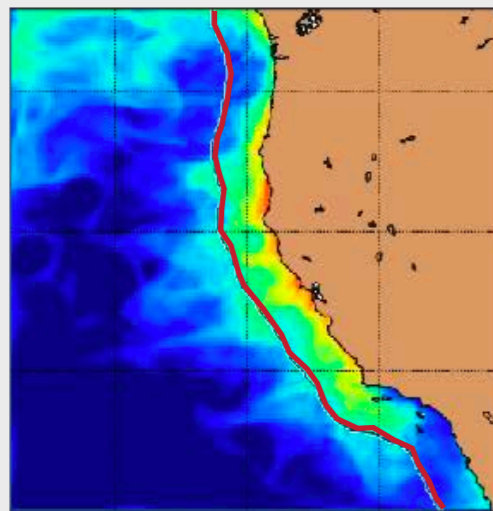


# RESULT: SURFACE CHLOROPHYLL BEFORE DATA ASSIMILATION

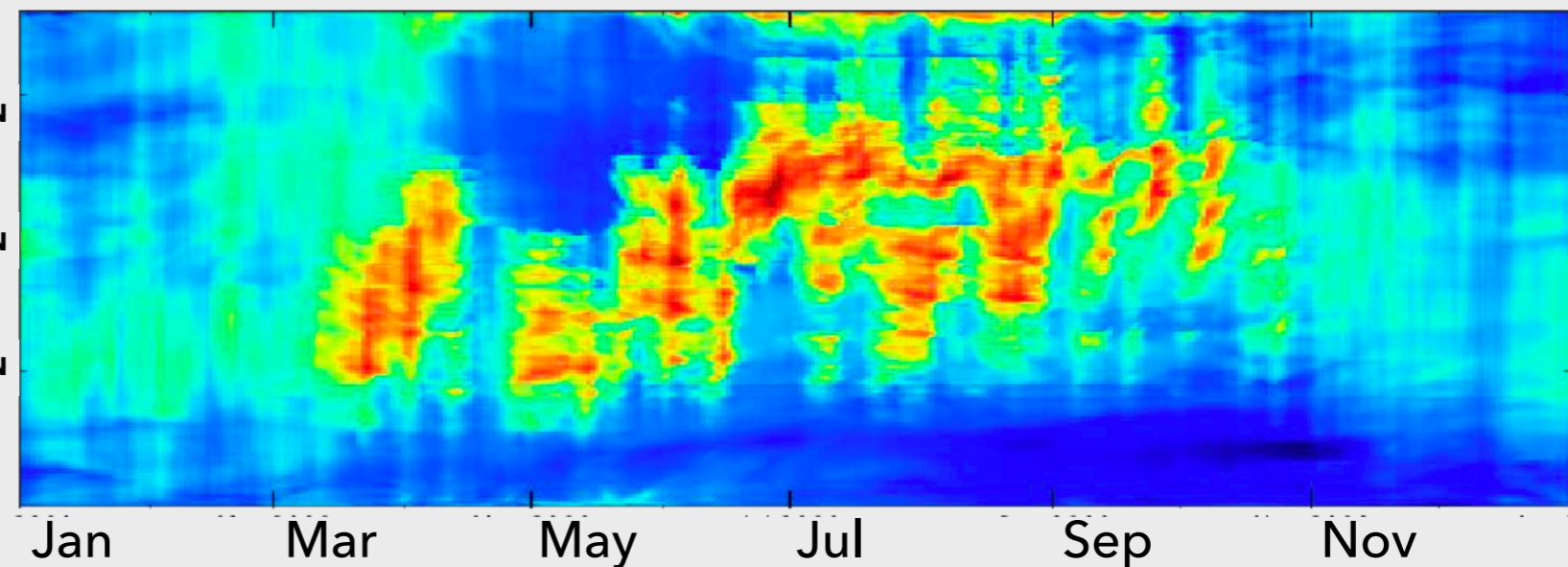
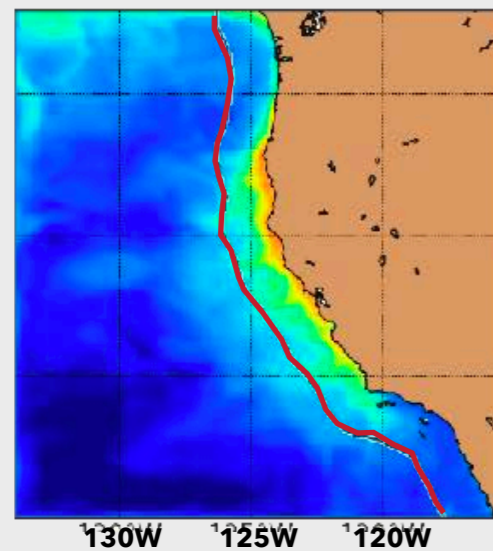
SeaWiFS



NPZD, Free



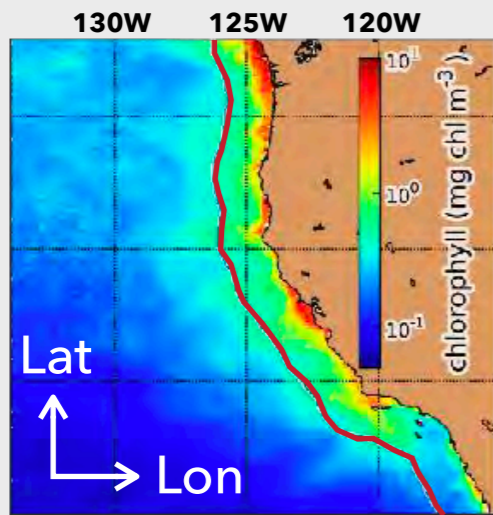
NEMURO, Free



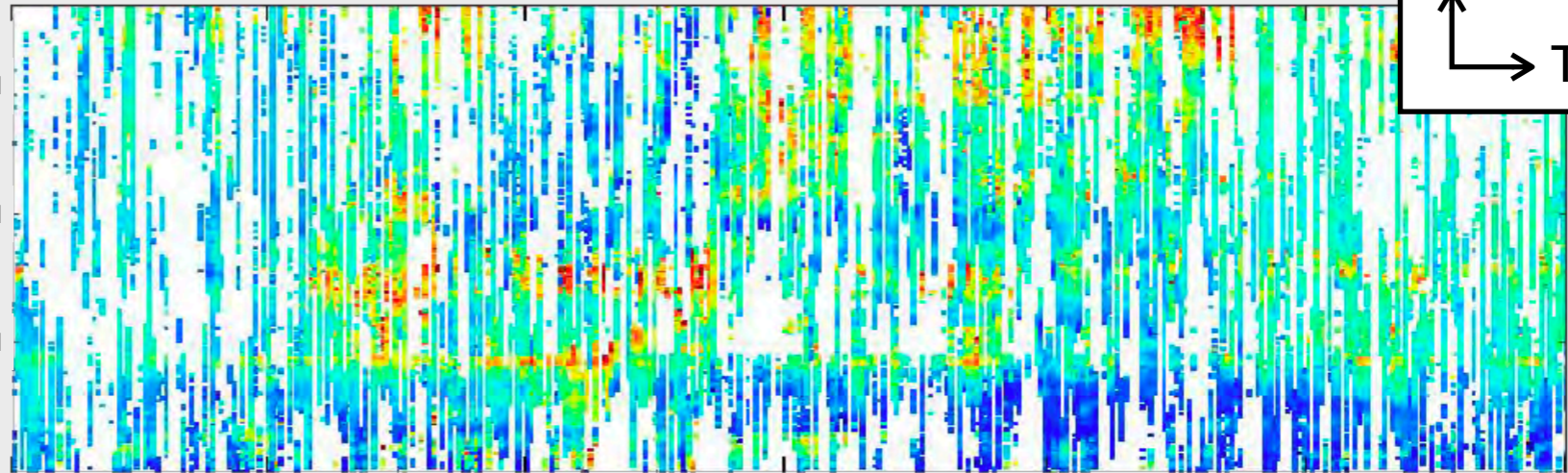


# RESULT: SURFACE CHLOROPHYLL AFTER DATA ASSIMILATION

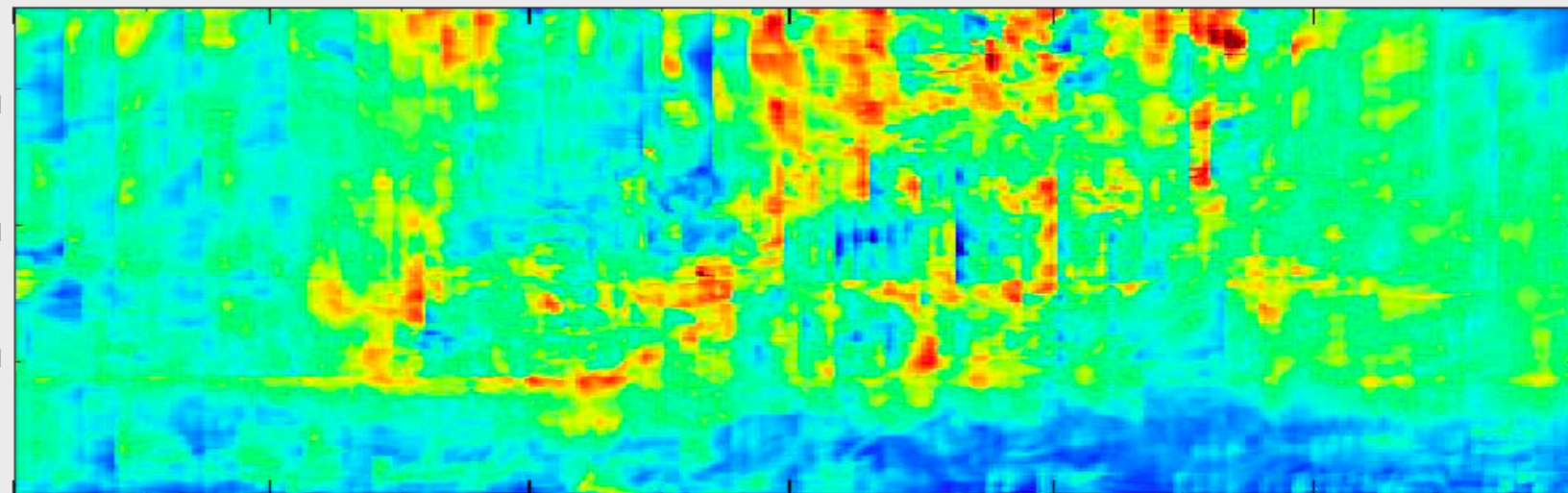
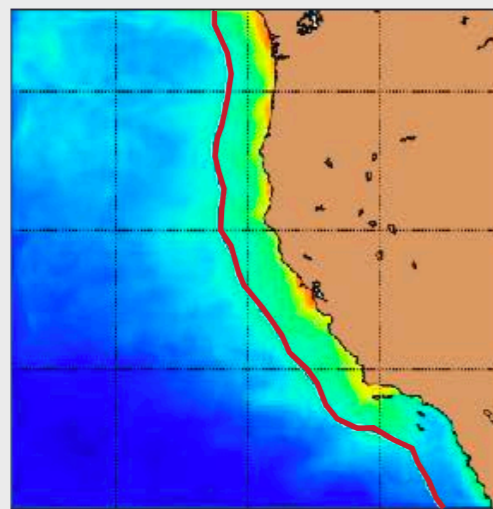
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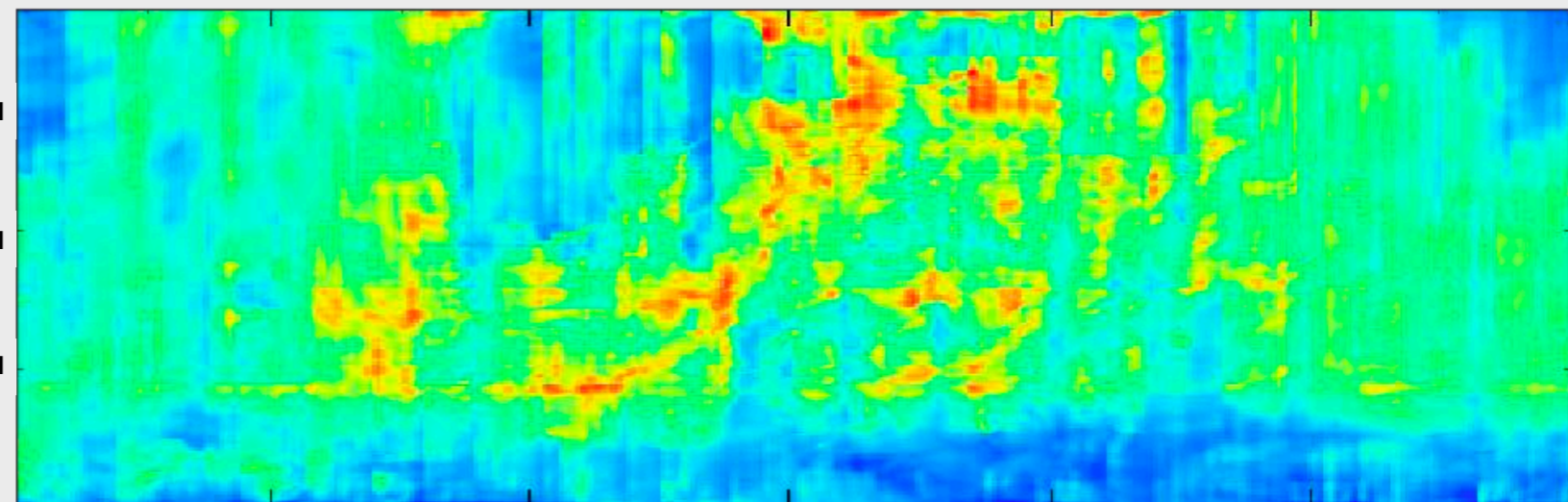
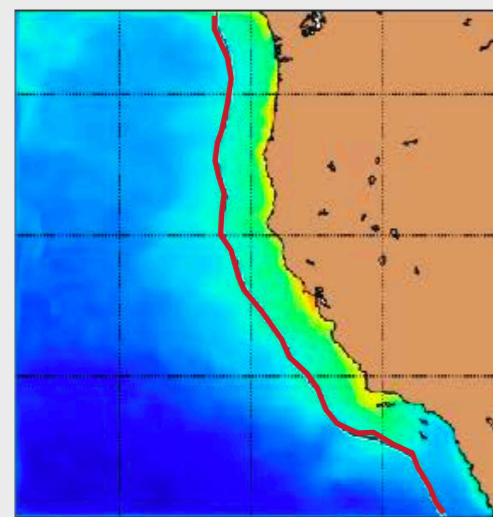
200 km



NPZD, DA



NEMURO, DA



Jan

Mar

May

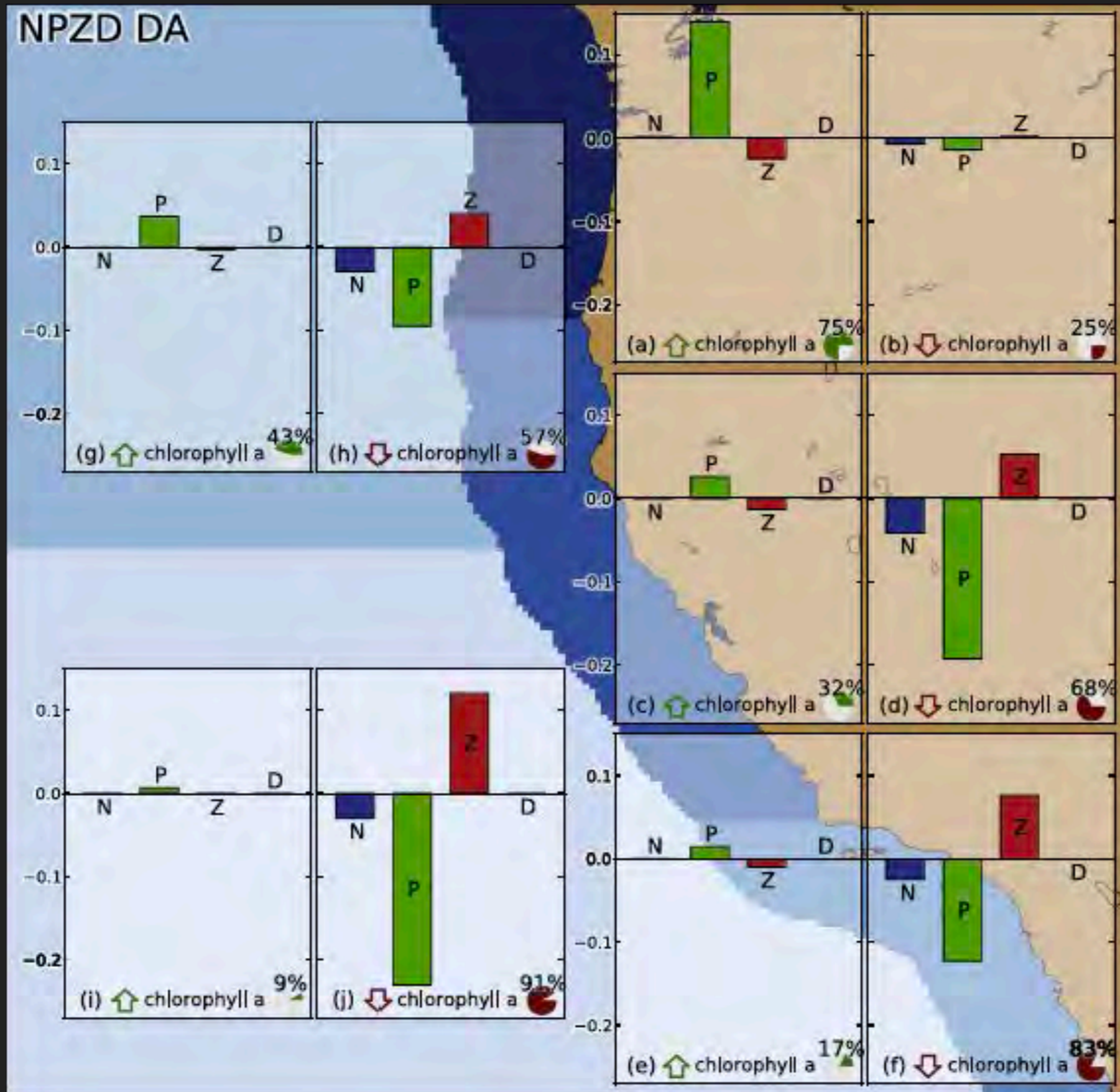
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Sep

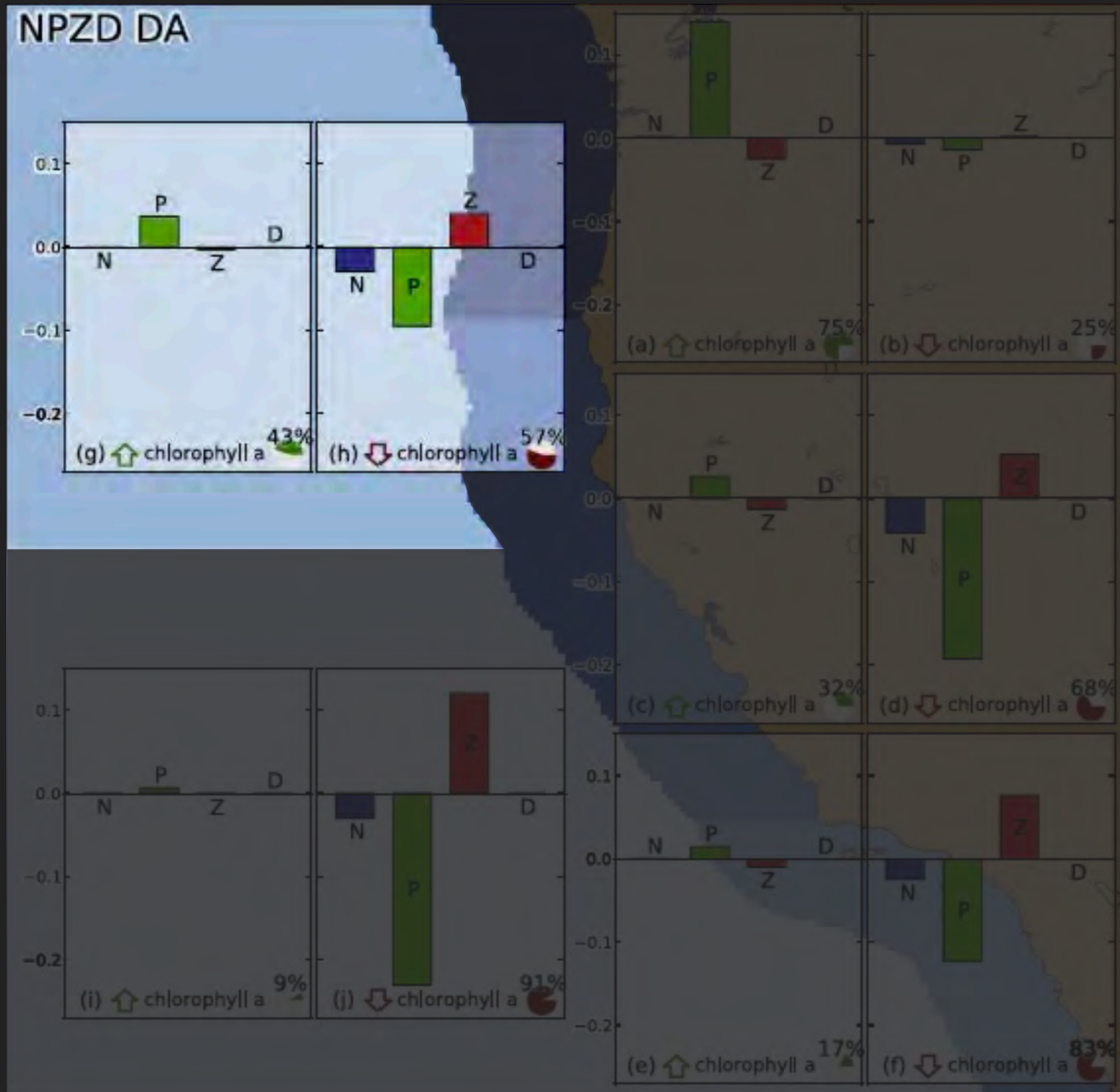
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# RESULT: HOW THE MODEL FITS THE DATA?: NPZD MODEL

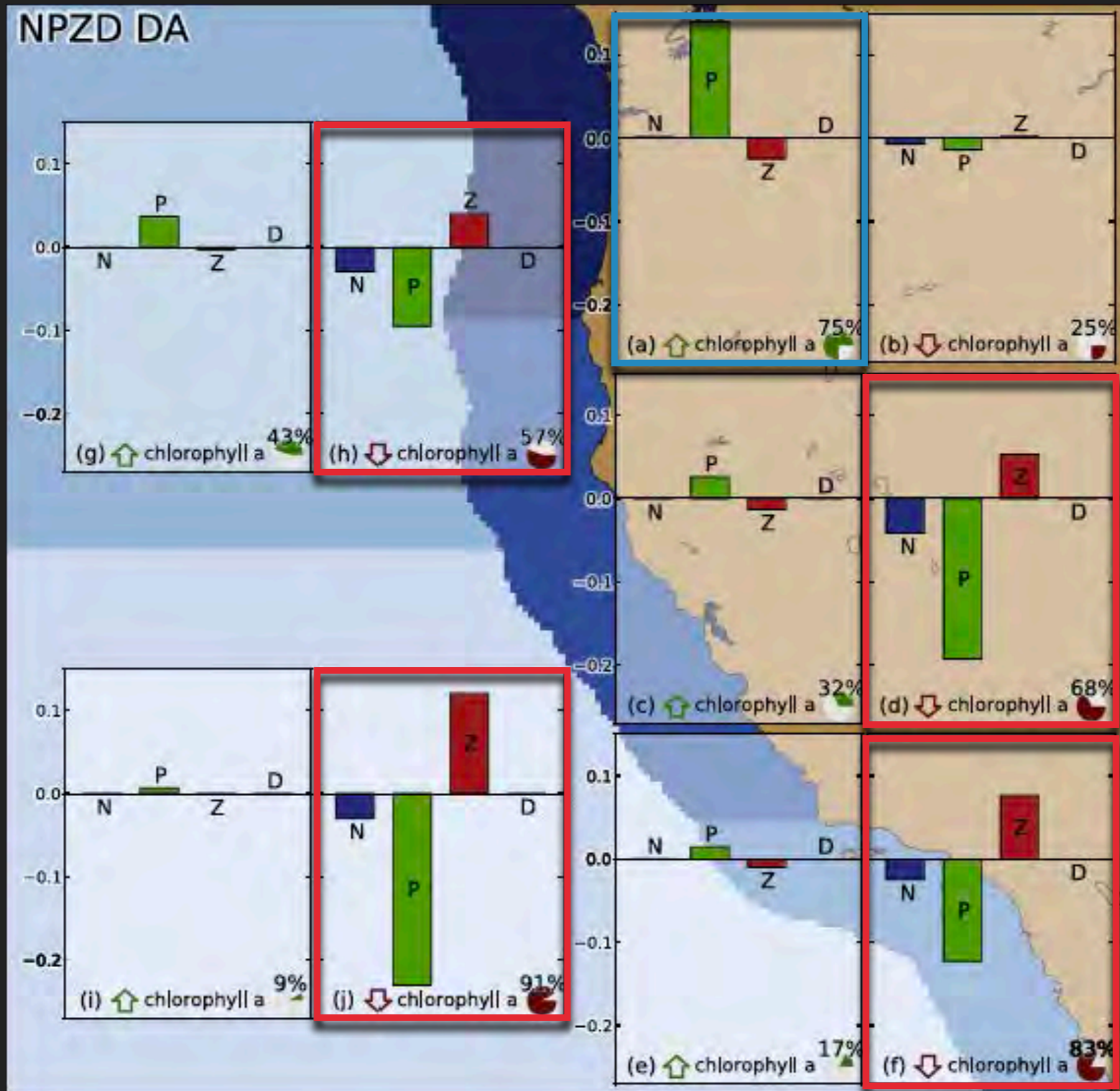


# RESULT: HOW THE MODEL FITS THE DATA?: NPZD MODEL

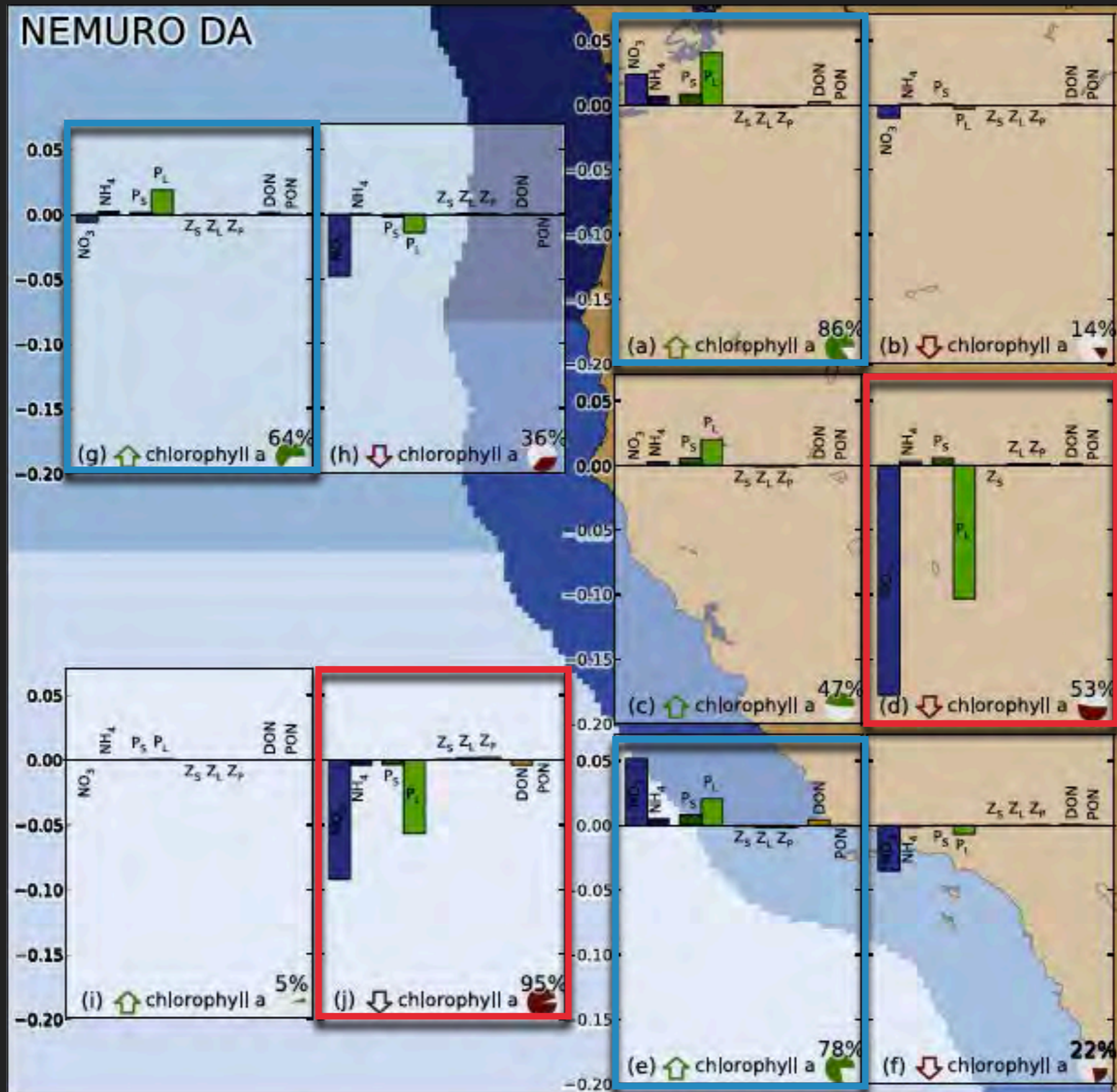




# RESULT: HOW THE MODEL FITS THE DATA?: NPZD MODEL

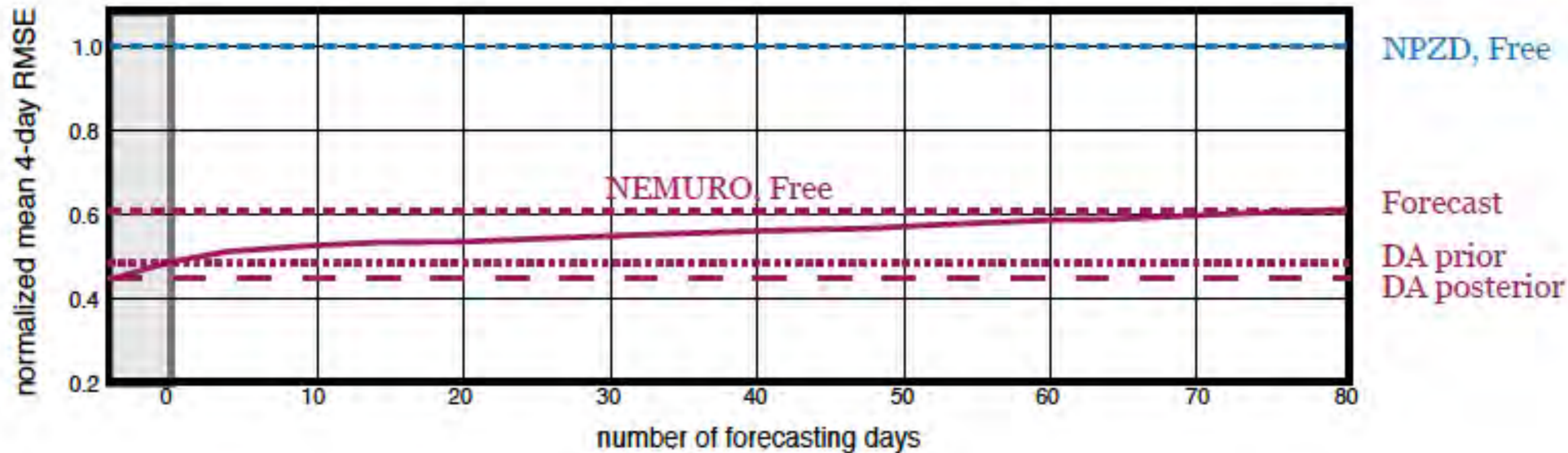
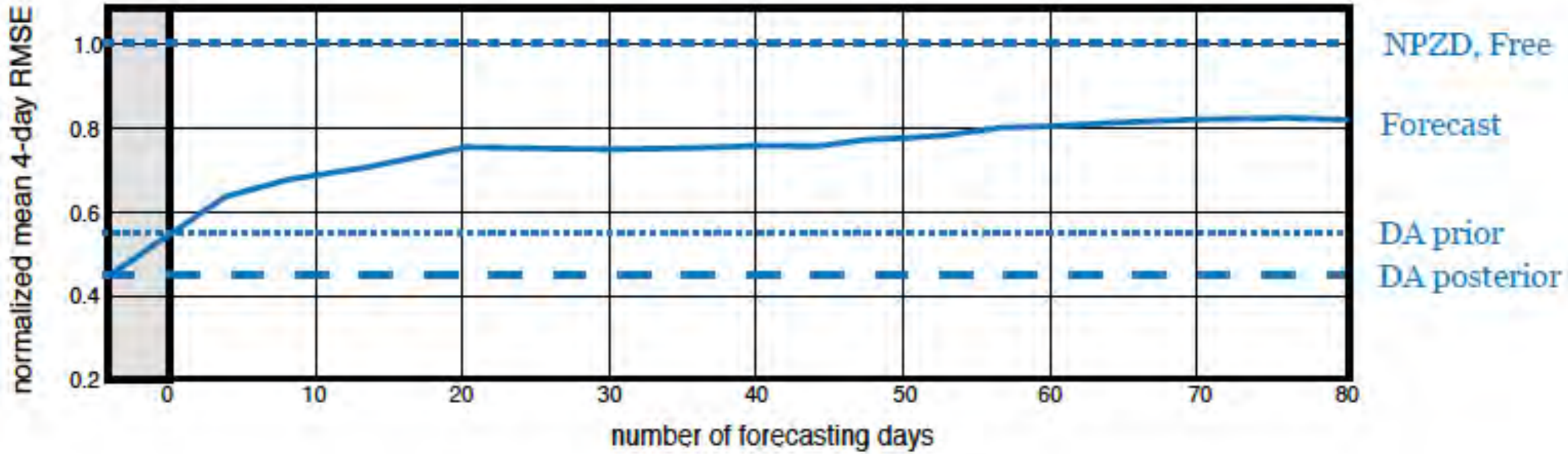


# RESULT: HOW THE MODEL FITS THE DATA?: NEMURO MODEL





# RESULT: FORECAST



## SUMMARY

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- ▶ Coupled physical-biogeochemical data assimilation
- ▶ Both NPZD and NEMURO fit the satellite chlorophyll data.
- ▶ The coupled DA system works! (but depends on **B** as always)

### NPZD

### NEMURO

Simpler

More complex

Adjusting P and Z

Adjusting N and P

Lower forecast skill

Higher forecast skill

Longer memory from abs

Shorter memory from abs